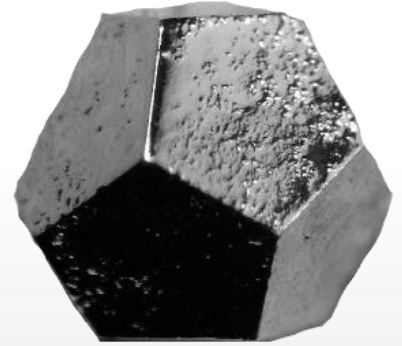




AGH UNIVERSITY OF SCIENCE
AND TECHNOLOGY



Effect of Magnetism on Lattice Dynamics: Mössbauer Spectroscopic View

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INTRODUCTION (1)

- ◆ Figure of merit, adiabatic parameter (standard EPI theory):

$$\gamma = h \nu_D / E_F \sim (m/M)^{1/2} \ll 1 \quad (1)$$

(ν_D is the Debye frequency, E_F is the Fermi energy, m and M are the electron and ion masses, respectively).

(1) → Effect of magnetism on lattice vibrations is negligible.

- ◆ Kim's theory [1]:

For itinerant ferromagnetmagnets the effect can be enhanced by a factor of up to $\sim 10^2$.

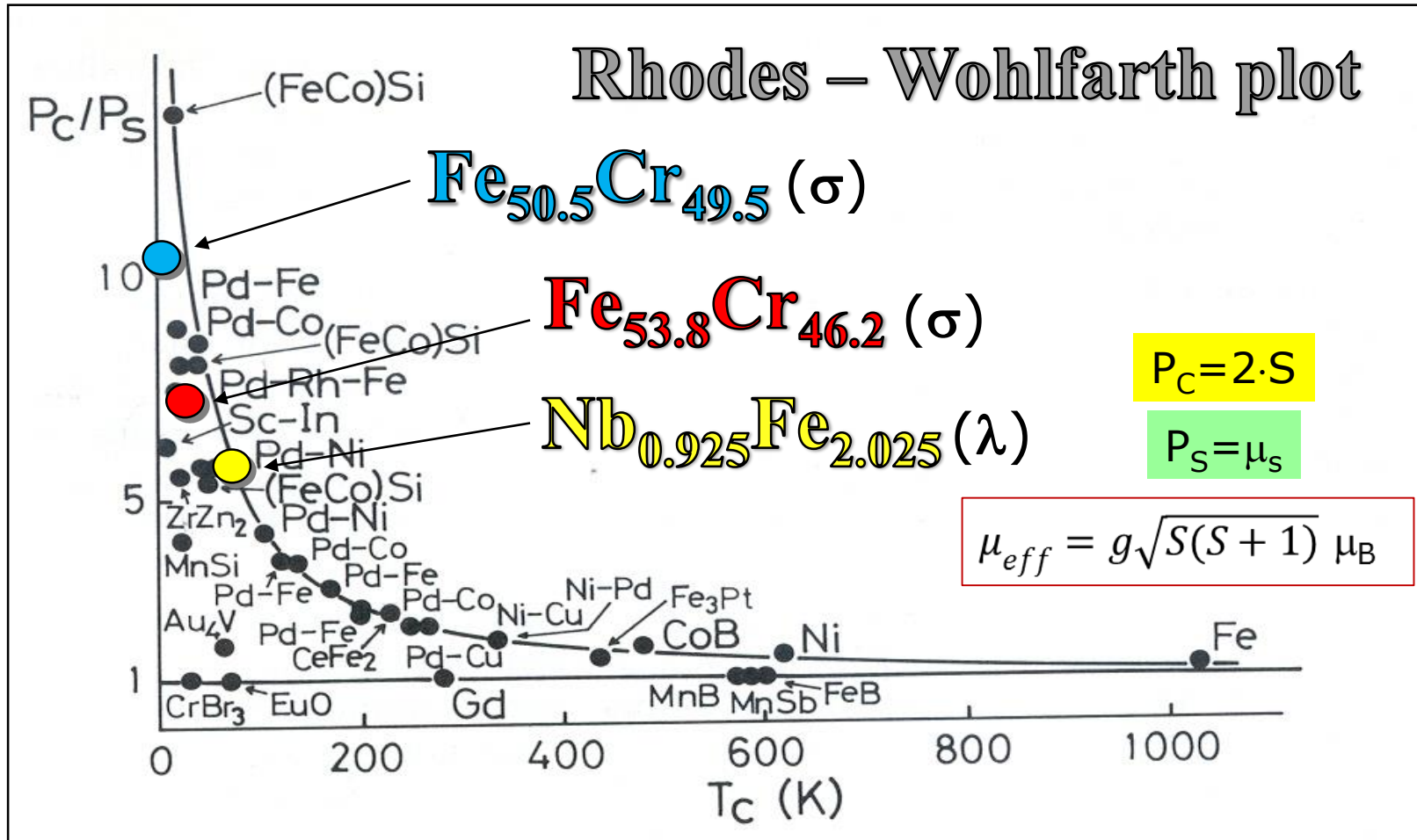
INTRODUCTION (2)

Controversies over the standard EPI theory (examples):

- ◆ *This theory neglects the effect of magnetism on lattice dynamics and fails to explain enhancement of the critical temperature in phonon-mediated superconductors (I. S. Tupitsyn et al., PRB, 94 (2016) 155145).*
- ◆ *Lattice vibrations strongly affect the distribution of local magnetic moment in paramagnetic Fe viz. they weaken their mean values (B. Alling et al., PRB, 93 (2016) 224411).*
- ◆ *The PDOS of bcc Fe-V alloys across the full composition range were studied by inelastic neutron scattering, nuclear resonant inelastic x-ray scattering, and ab initio calculations. Changes in the PDOS were revealed at crossing the Curie temperature (M. S. Lucas et al., PRB, 82, (2010) 144306).*

RHODES-WOHLFARTH CRITERION

- ◆ Ferromagnet is itinerant if $P_C/P_S > 1$

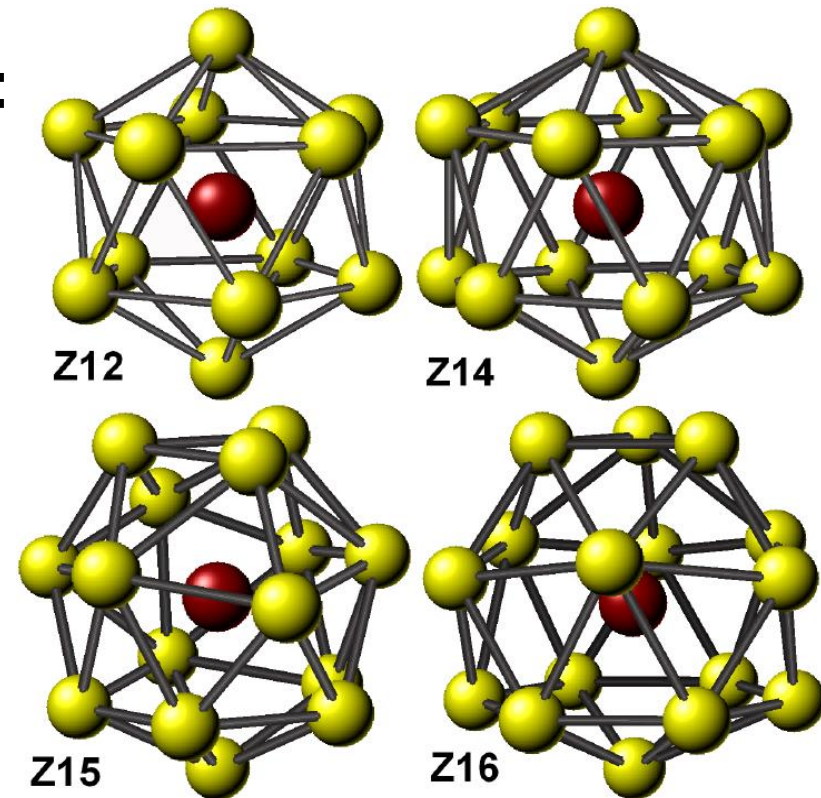


EXAMPLES TO BE PRESENTED

- ◆ Frank-Kasper or Topologically Close-Packed (TCP) Phases:
 - σ -phase: Fe-Cr and Fe-V
 - λ -phase (Laves): NbFe₂
- ◆ Chromium:
 - S.C. Cr(¹¹⁹Sn)-ISDW and Cr3%Mn(¹¹⁹Sn)-CSDW (AF)
 - Polycrystalline Cr (⁵⁷Fe)

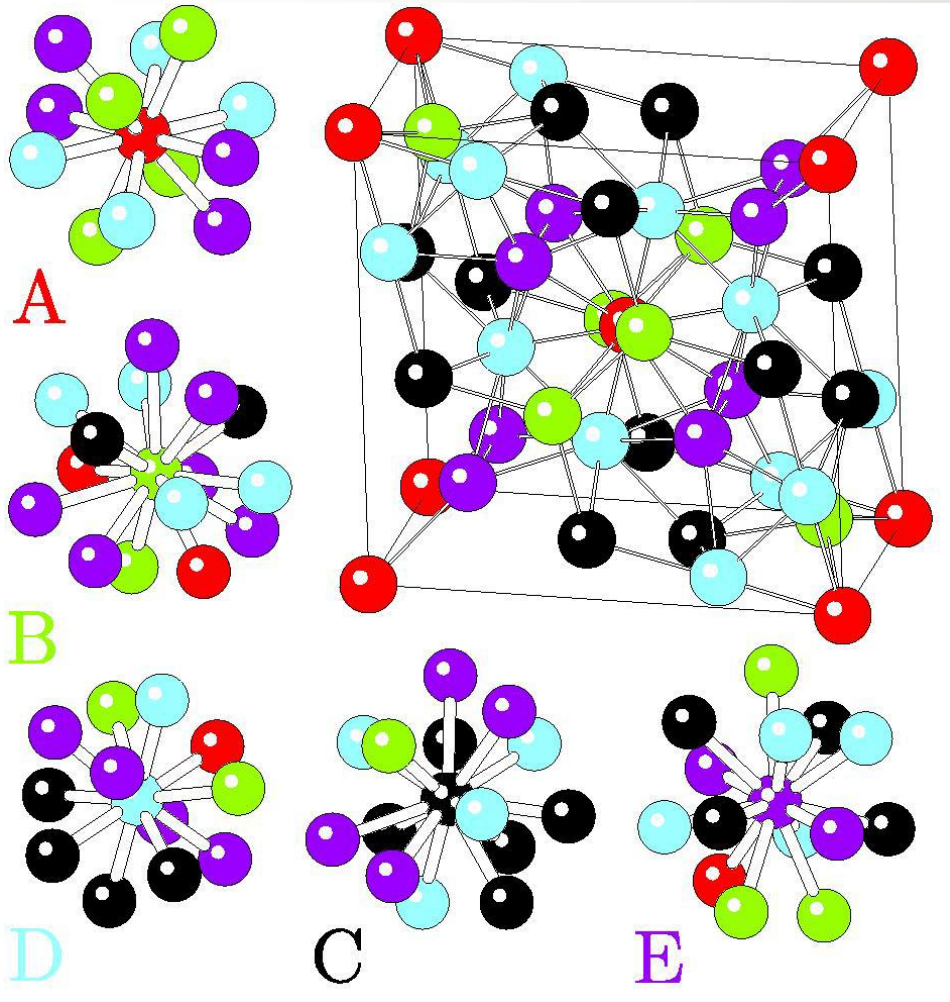
FRANK-KASPER PHASES

- Intermetallic compounds with high coordination numbers (CN): $12 \leq \text{CN} \leq 16$.
- Most popular F-K: A15, λ (Laves), σ , μ , χ , M, P, and R.
- Complex unit cell with ≥ 2 lattice sites and many atoms e.g. $\lambda(3)$, $\mu(13)$, $\sigma(30)$, M(52), R(53), P(56).
- Different physical properties depending on a compound's constitution and composition: A15 (Nb_3Sn) superconductive.

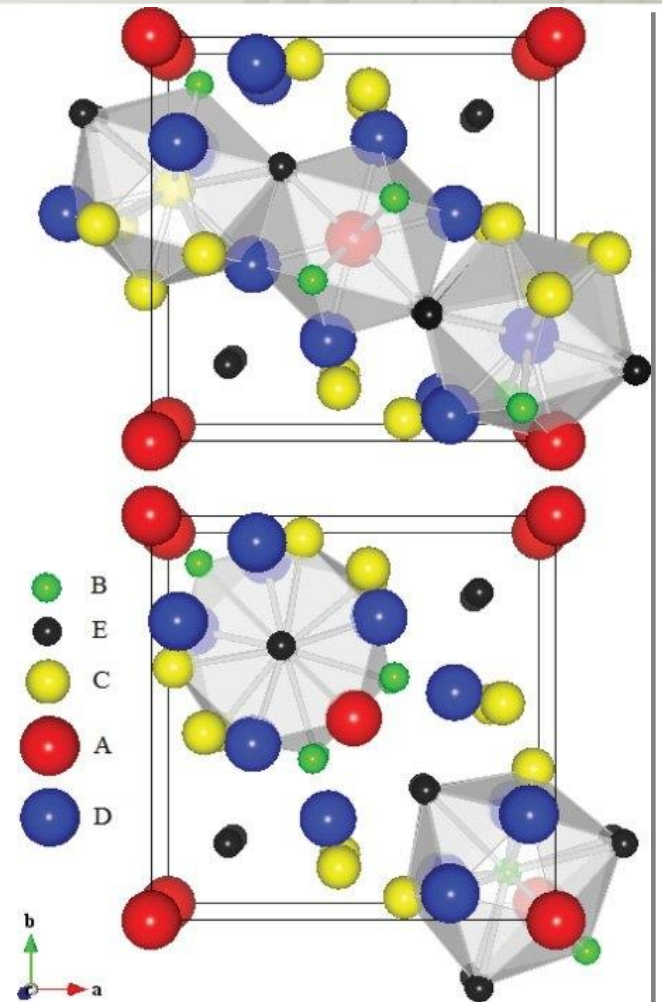


UNIT CELL

σ



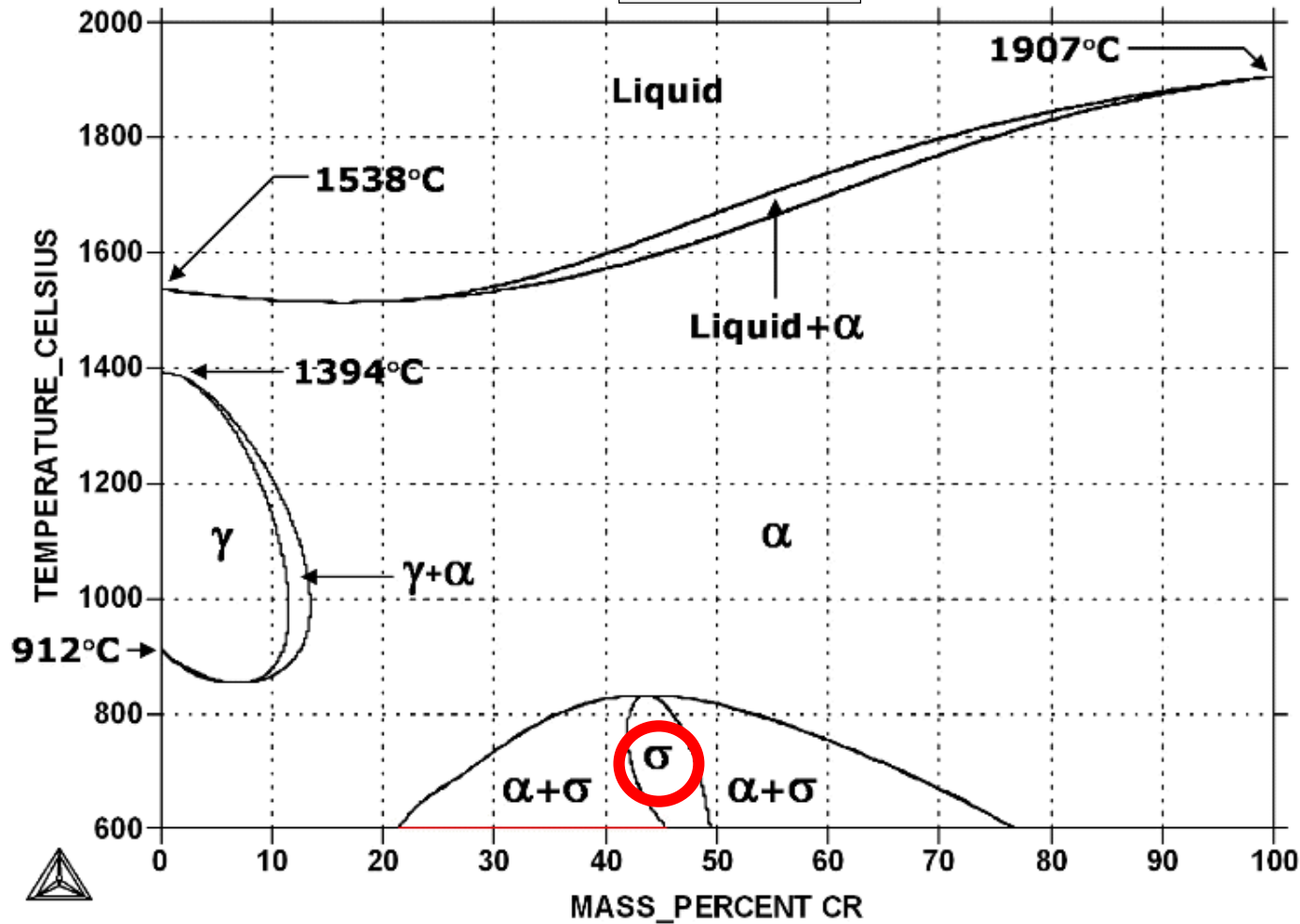
J. Cieslak et al., PRB (2010)



P. Blaha et al., PRB (2011)

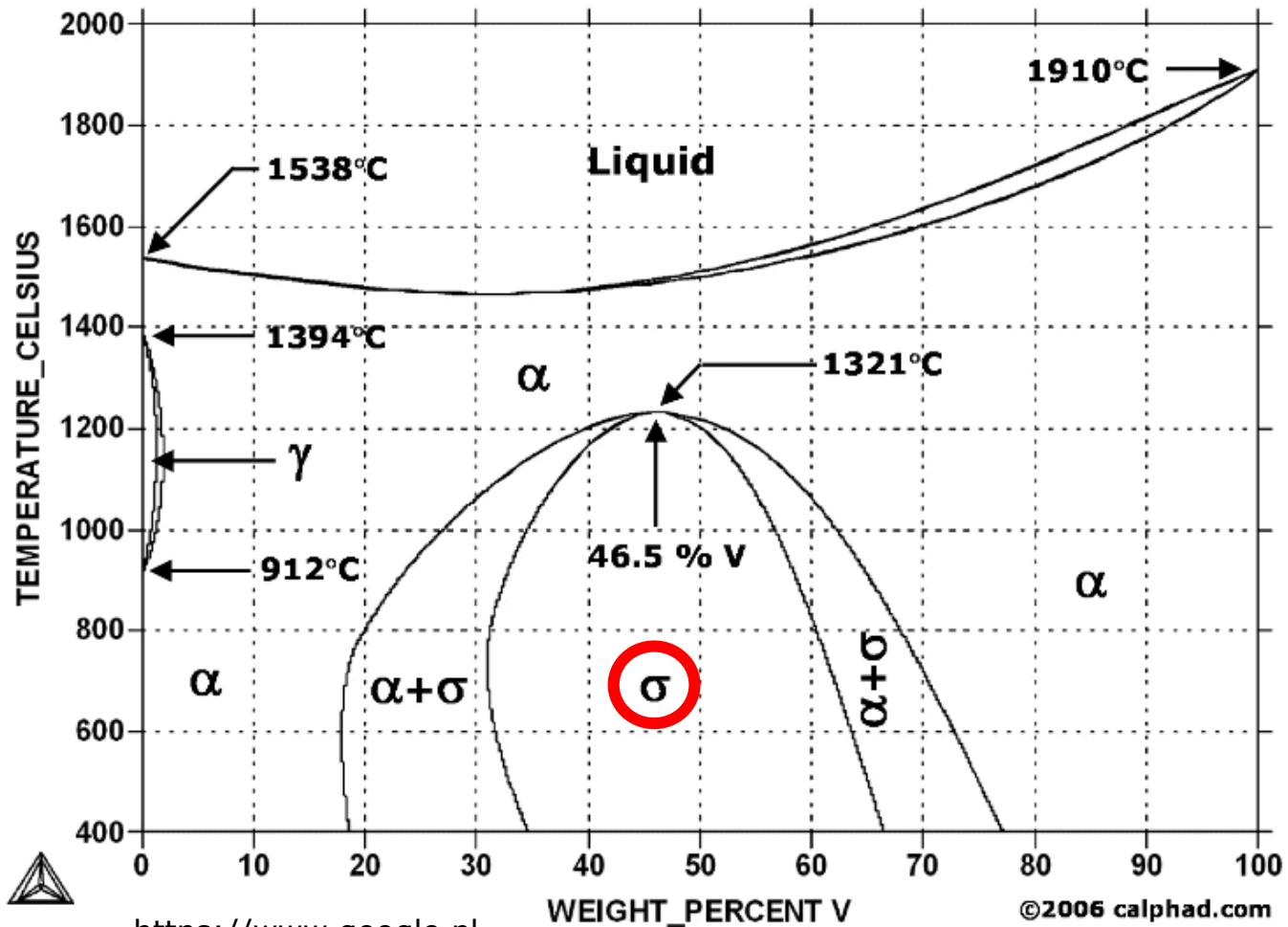
CRYSTALLOGRAPHIC PHASE DIAGRAM

Fe-Cr



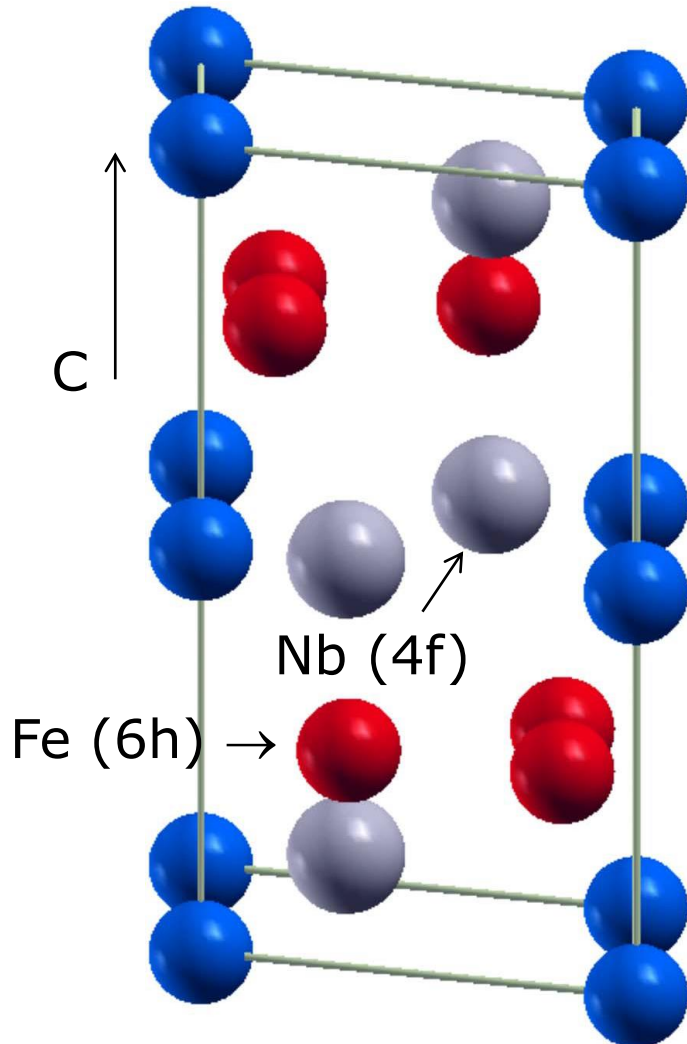
CRYSTALLOGRAPHIC PHASE DIAGRAM

Fe-V

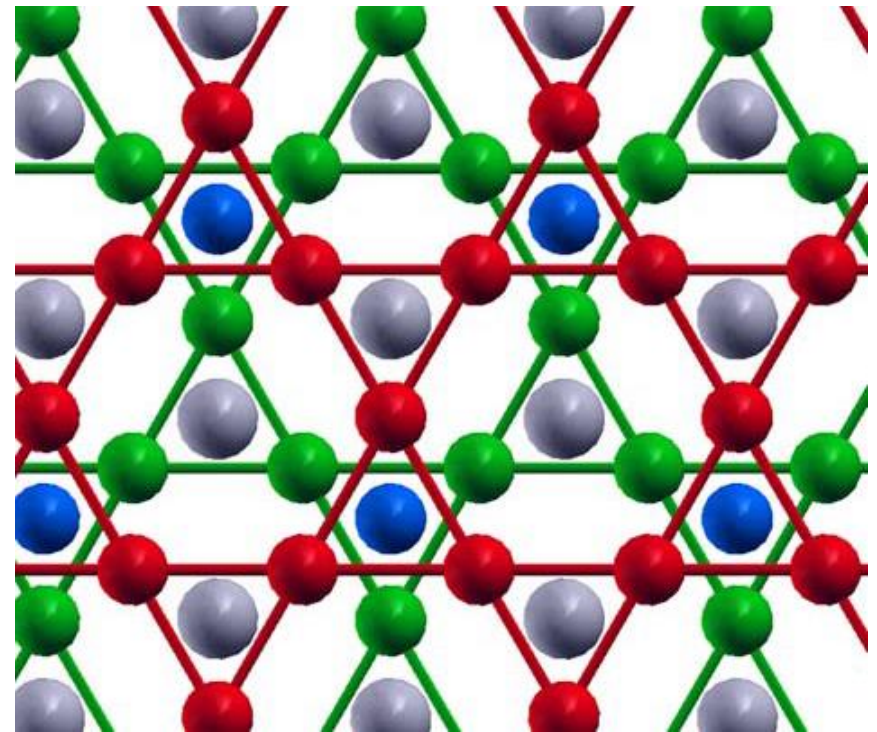


UNIT CELL

λ (C14)

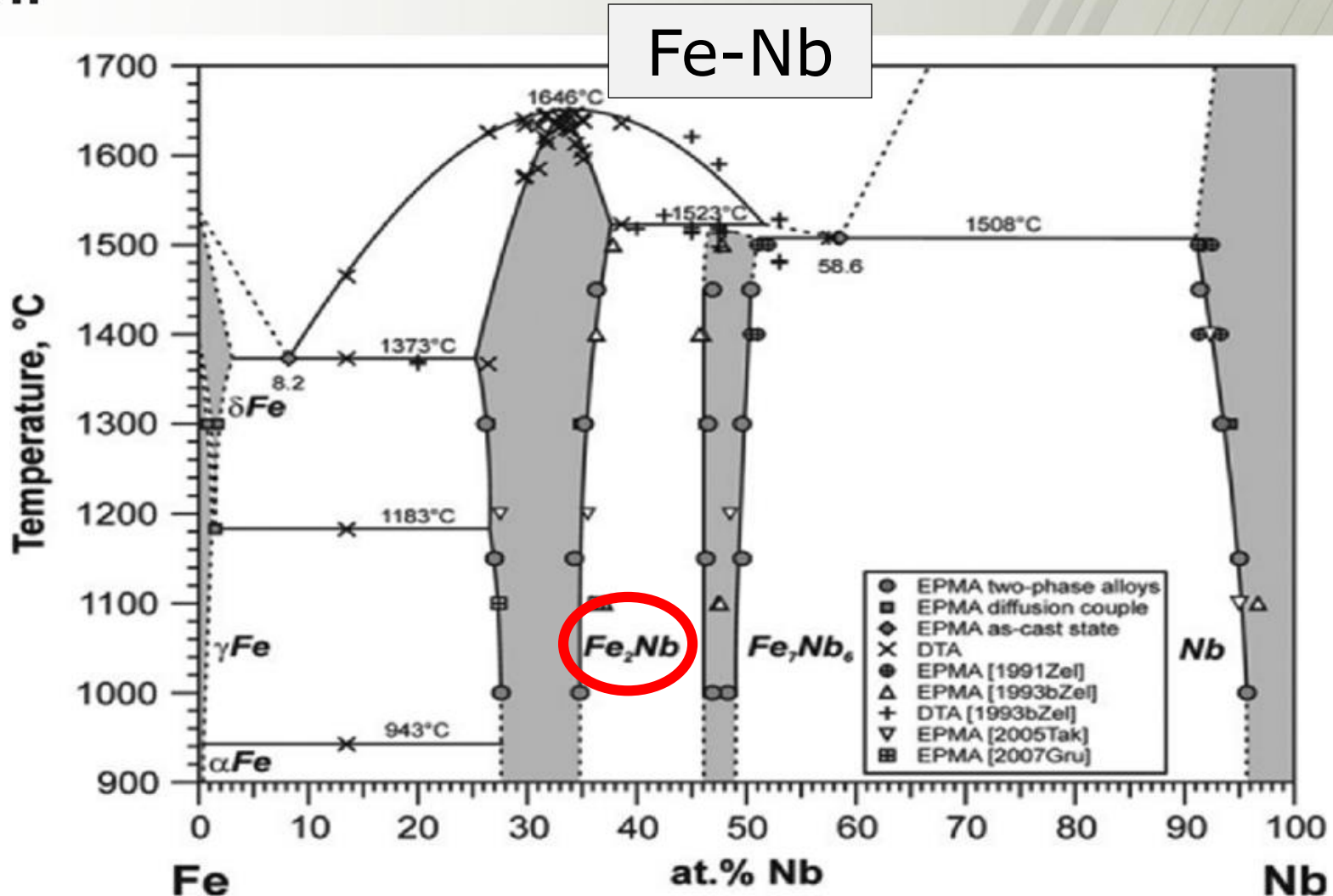


$2a:6h = 1:3$

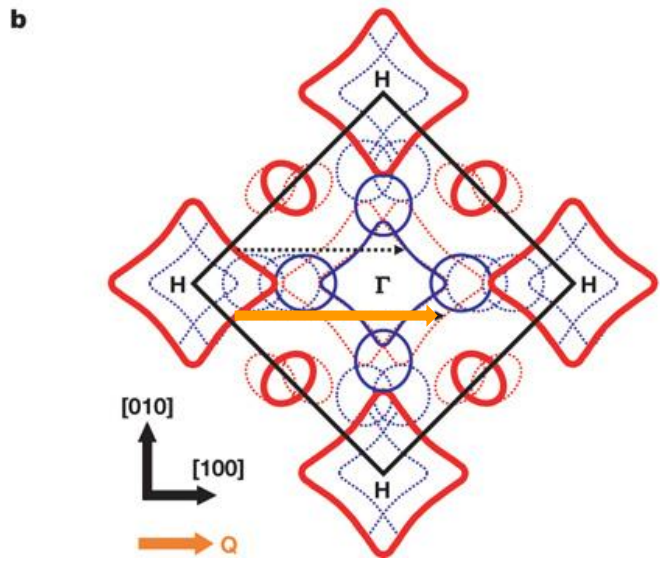
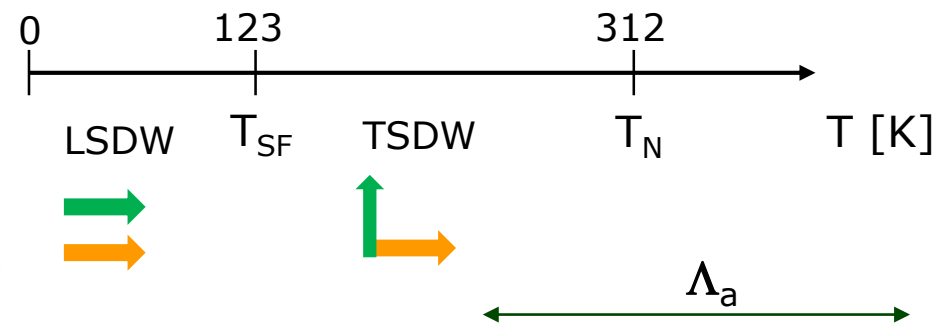
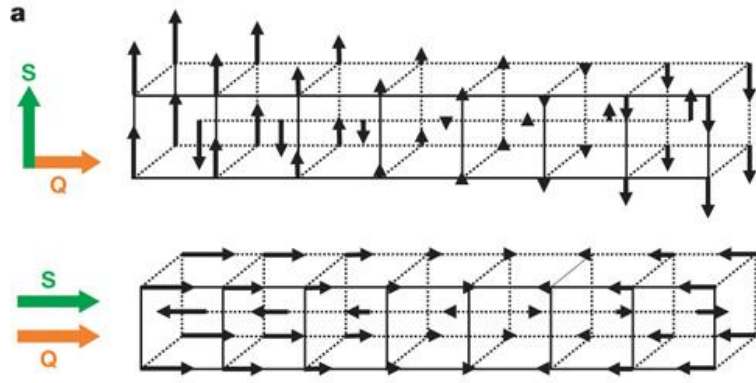


View \perp c

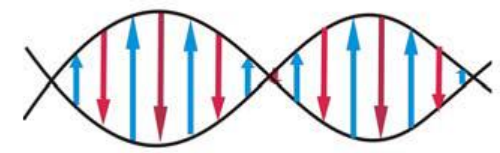
CRYSTALLOGRAPHIC PHASE DIAGRAM



CHROMIUM - ISDW



$$\mu = \mu_1 \sin Qr$$



$$Q = \frac{2\pi(1-\delta)}{a}$$

$$\Lambda = \frac{2\pi}{Q} = \frac{a}{1-\delta}$$

$$\Lambda_a = \frac{a}{\delta}$$

T[K]	Λ_a [a]	Λ_a [Å]
4	~20	~57
312	~27	~78

◆ Mössbauer spectroscopy:

$$SOD = -\frac{E_\gamma}{2c^2} \langle v^2 \rangle$$



$$E_k = 0.5m \langle v^2 \rangle$$

$$f = e^{-k^2 \langle x^2 \rangle}$$



$$E_p = 0.5K^2 \langle x^2 \rangle$$

EXPERIMENTAL TOOLS

- ◆ Mössbauer spectroscopy (Debye model):

1. $CS(T) = IS(0) + SOD(T)$

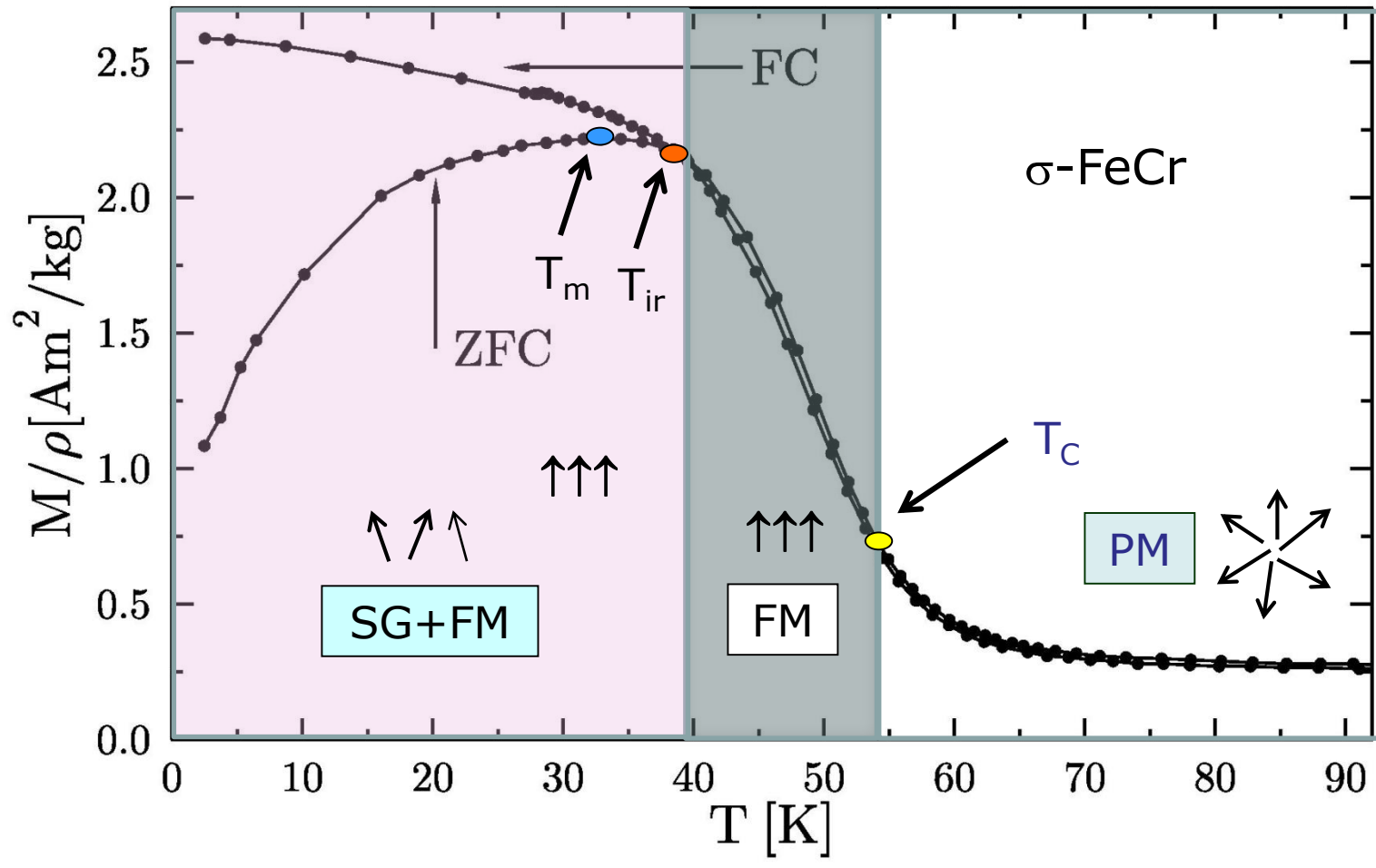
$$SOD(T) = \frac{3k_B T}{2mc} \left(\frac{3T_D}{8T} - 3 \left(\frac{T}{T_D} \right)^3 \int_0^{T_D/T} \frac{x^3}{e^x - 1} dx \right)$$

2. f -factor (spectral area)

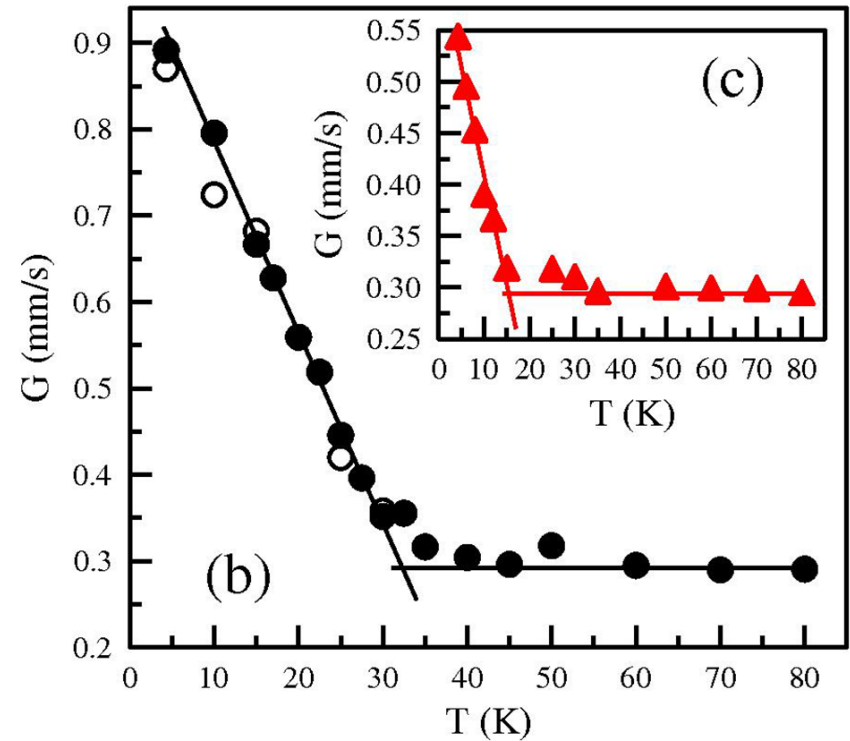
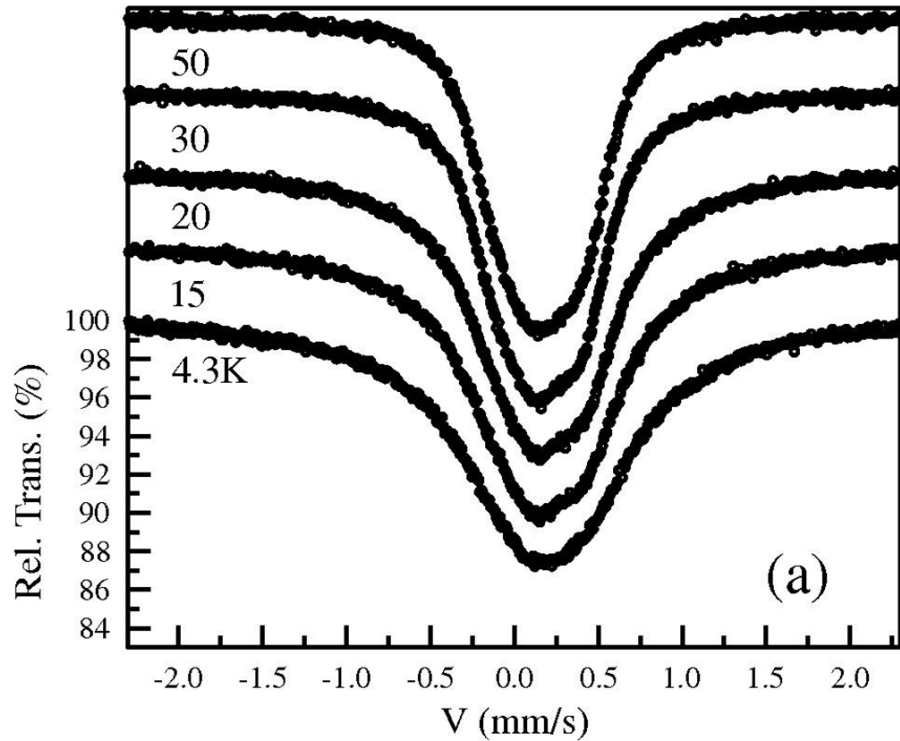
$$f = \exp \left[- \frac{6E_R}{k_B T_D} \left\{ \frac{1}{4} + \left(\frac{T}{T_D} \right)^2 \int_0^{T_D/T} \frac{x}{e^x - 1} dx \right\} \right]$$

RESULTS: σ -FeCr

- **Re-entrant type (PM \rightarrow FM \rightarrow SG+FM)**

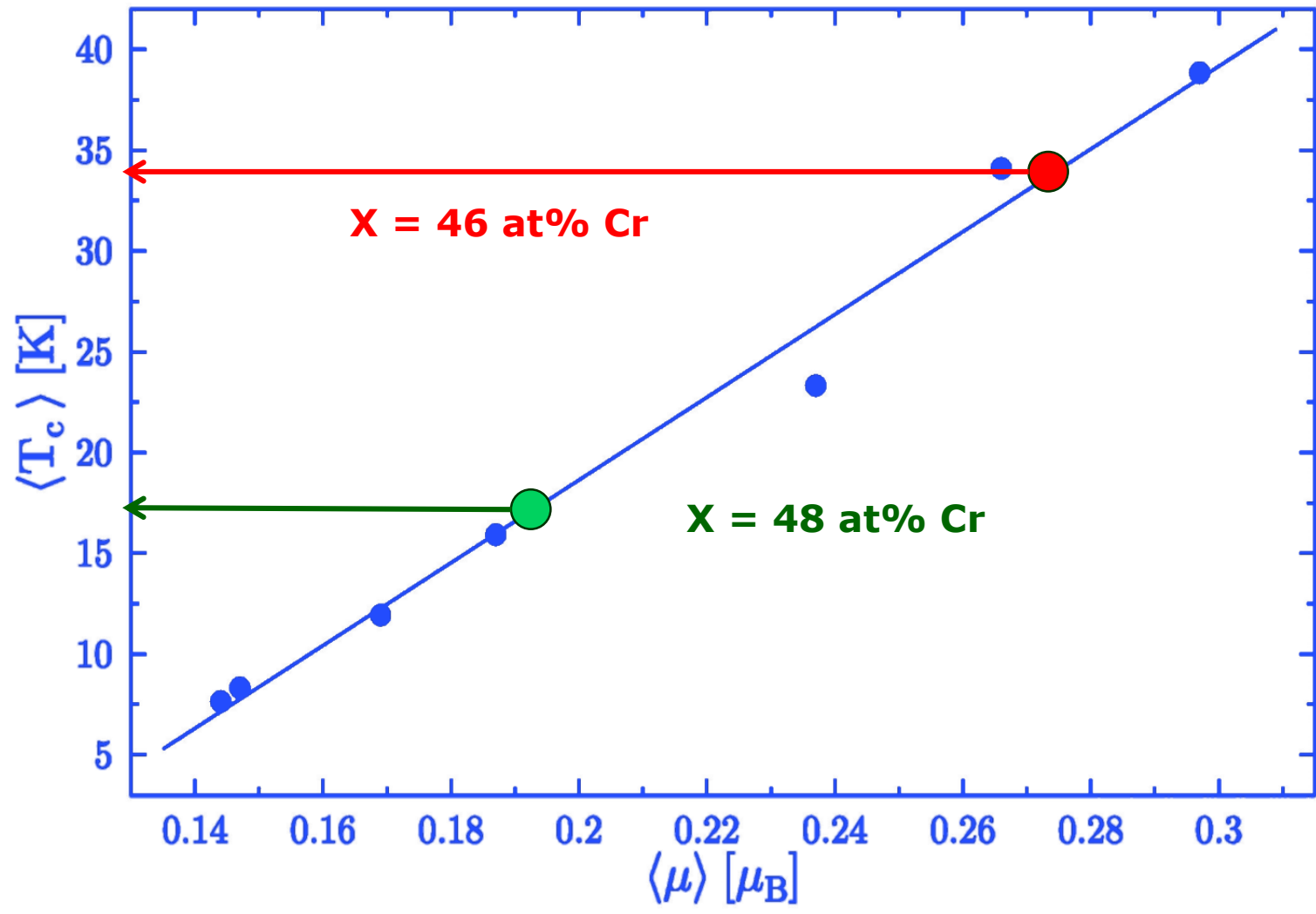


RESULTS: σ -FeCr

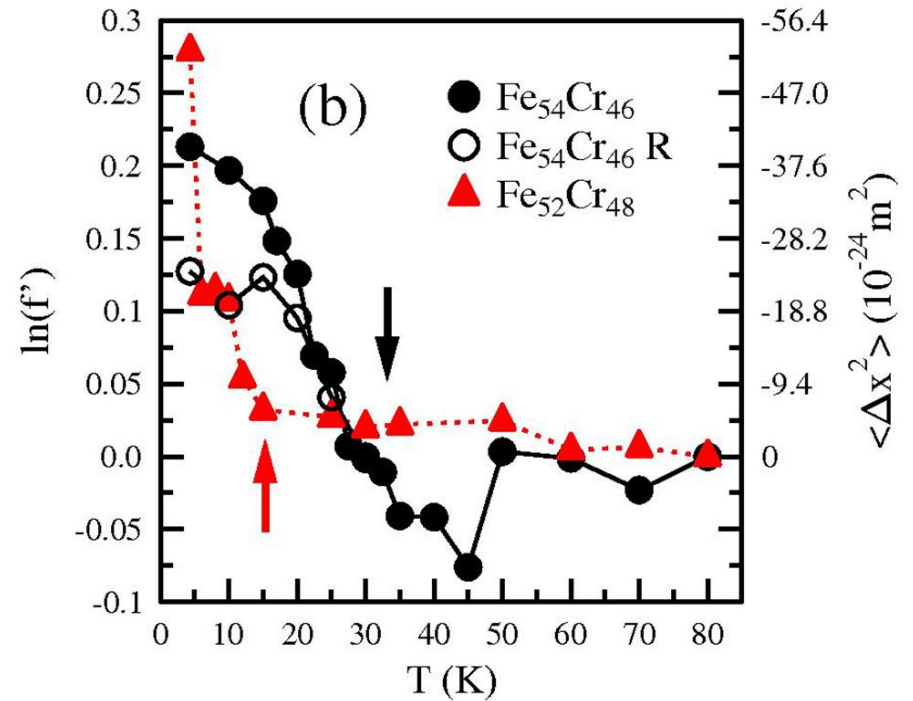
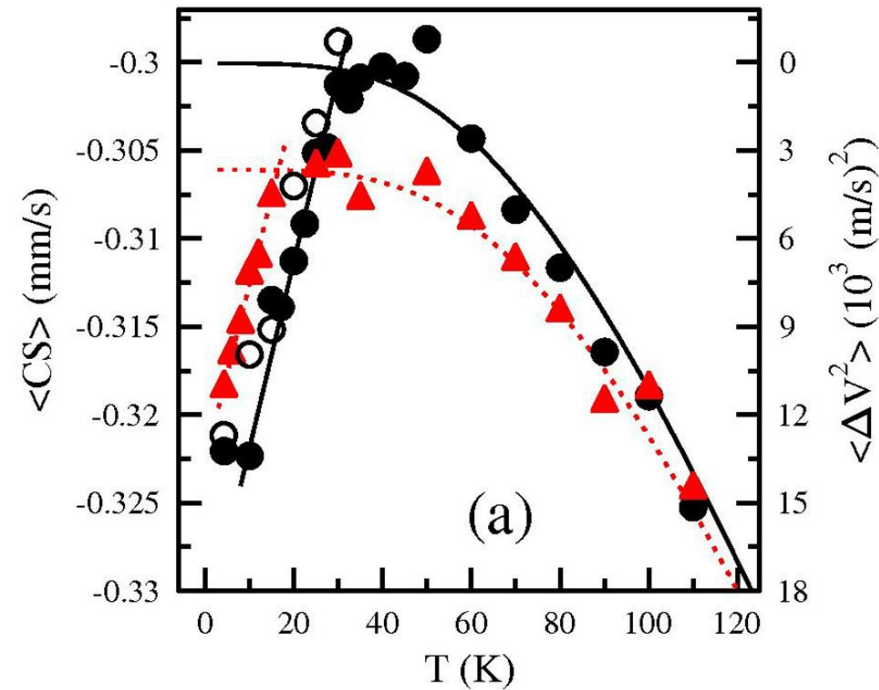


T_C : ~32 K for $x = 46$ at%Cr; ~15 K for $x = 48$ at% Cr

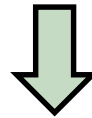
RESULTS: σ -FeCr



RESULTS: σ -FeCr



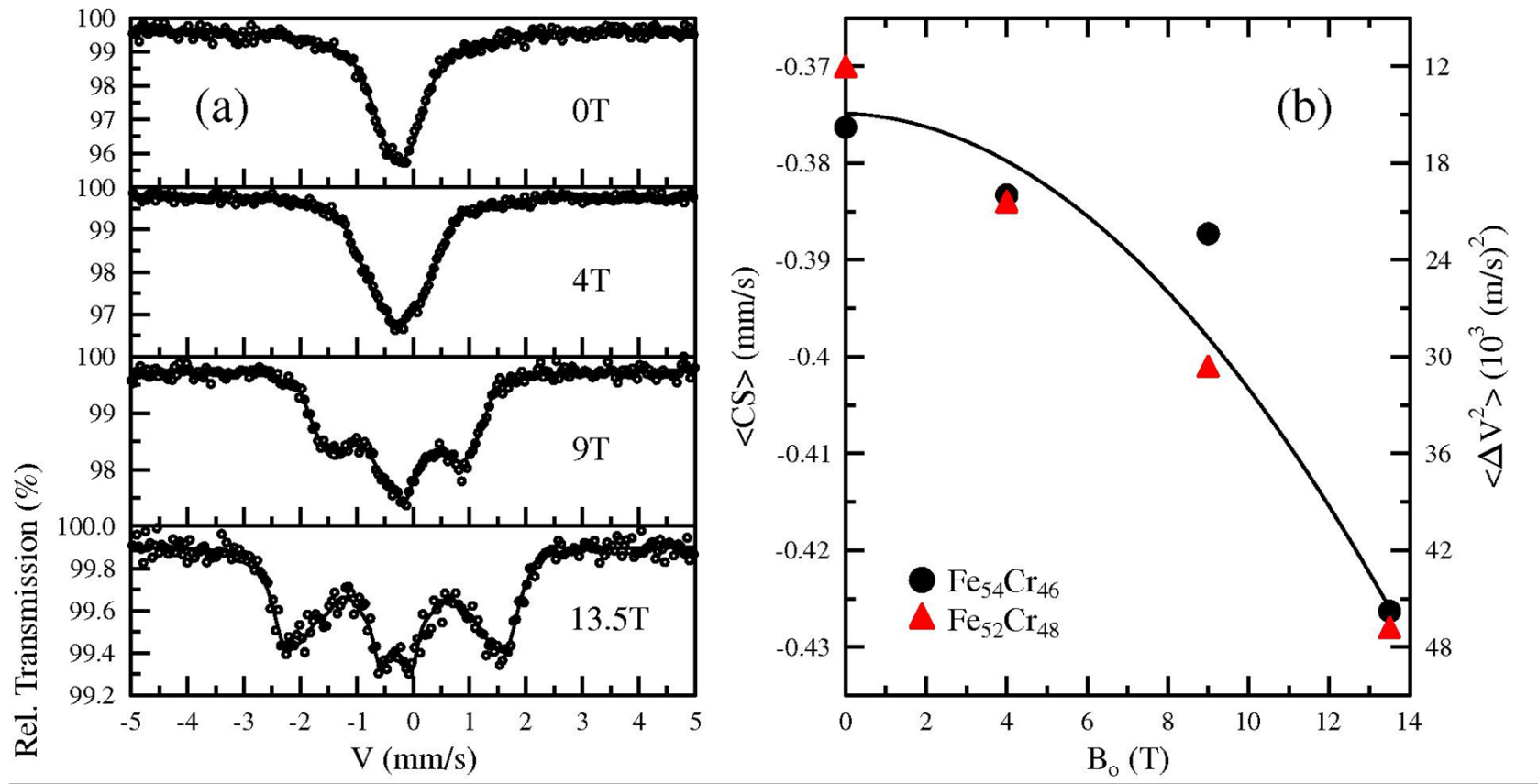
$$\langle CS \rangle = -0.5 E_{\gamma} \langle v^2 \rangle / c^2$$



$$f = \exp(-k^2 \langle x^2 \rangle)$$

There are anomalies both in $\langle CS \rangle$ and in f at $T \approx T_C$

RESULTS: σ -FeCr



S. M. Dubiel et al., EPL, 101 (2013) 16008



$\langle CS \rangle$ follows the trend found from zero-field measurements

RESULTS: σ -FeCr

◆ Energetics of vibrations

- Harmonic approximation:

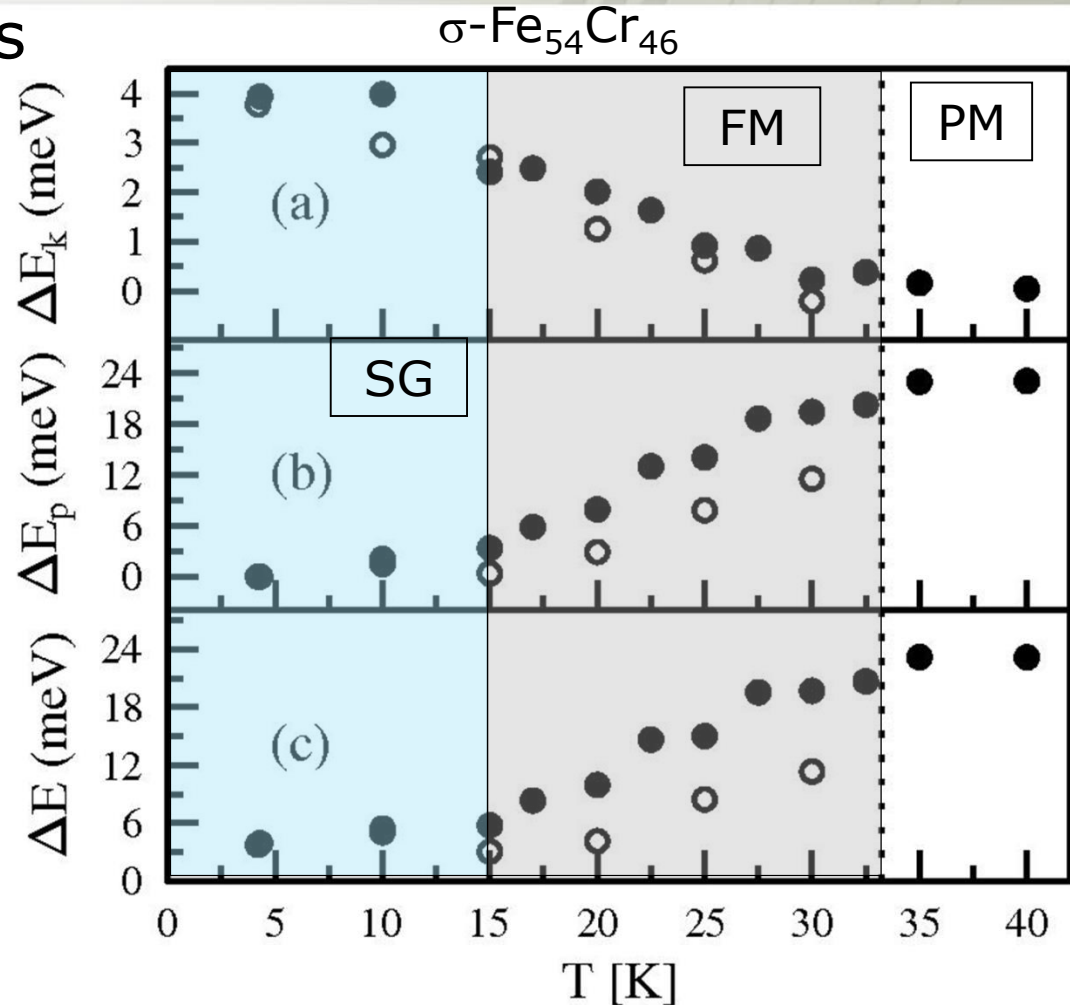
$$E = E_k + E_p$$

$$E_k = \frac{m \langle v^2 \rangle}{2}$$

$$E_p = \frac{K \langle x^2 \rangle}{2}$$

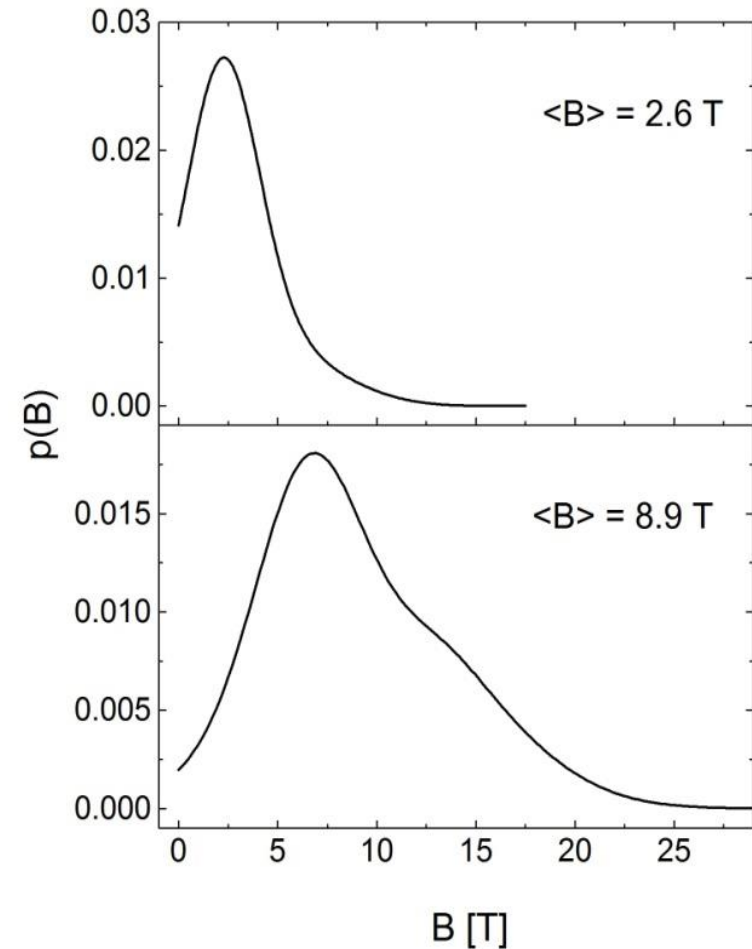
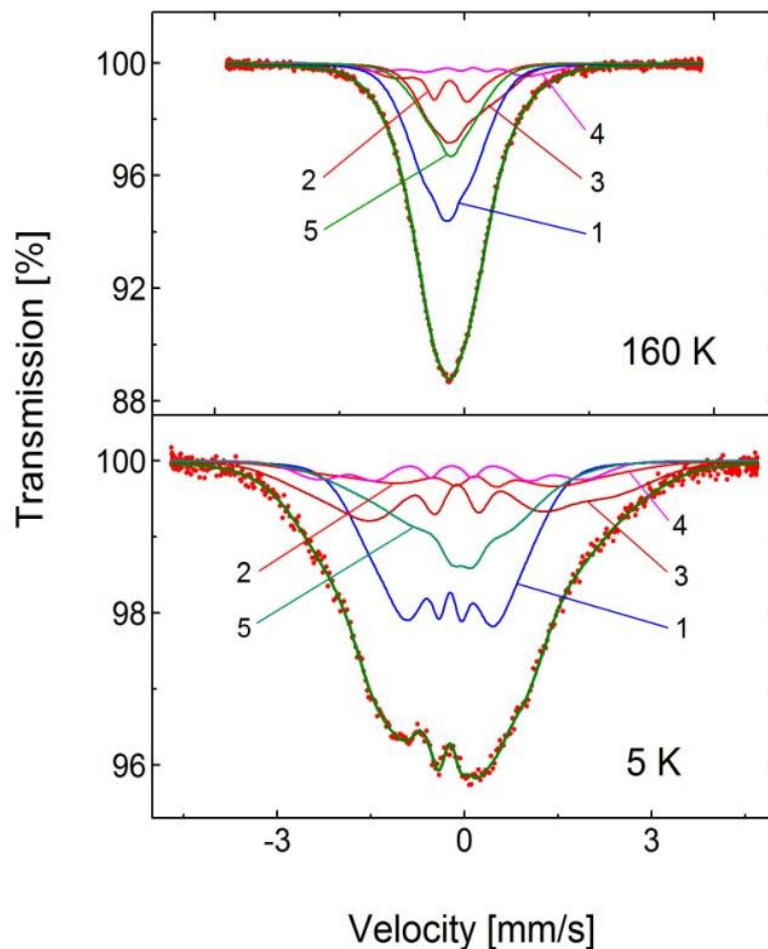
$$SOD = -\frac{E_\gamma}{2c^2} \langle v^2 \rangle \quad \rightarrow \quad \langle v^2 \rangle$$

$$f = \exp(-k^2 \langle x^2 \rangle) \quad \rightarrow \quad \langle x^2 \rangle$$

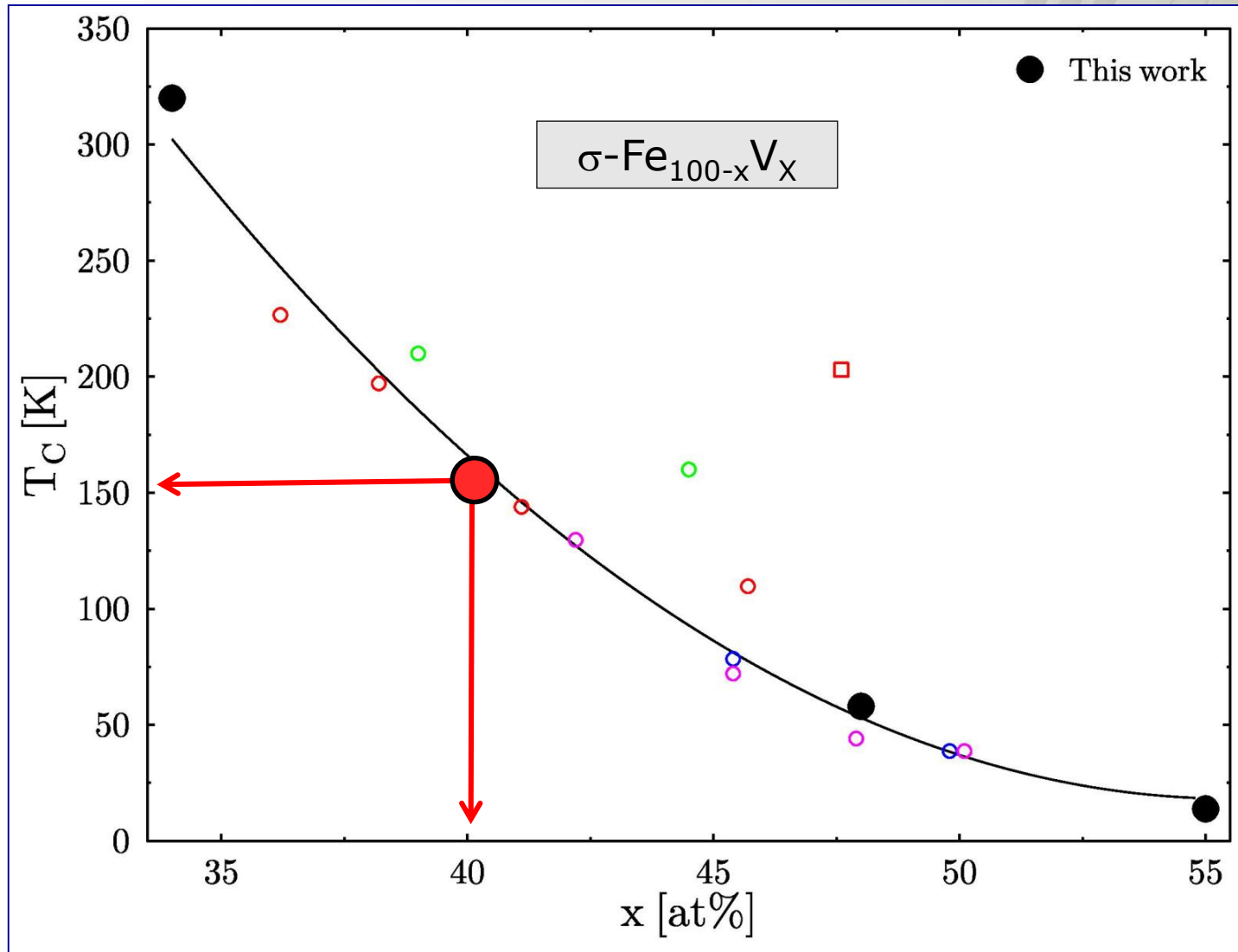


RESULTS: σ -FeV

- ◆ Mössbauer spectra: $x_v=40$ at% ($T_C \approx 160^\circ\text{C}$)

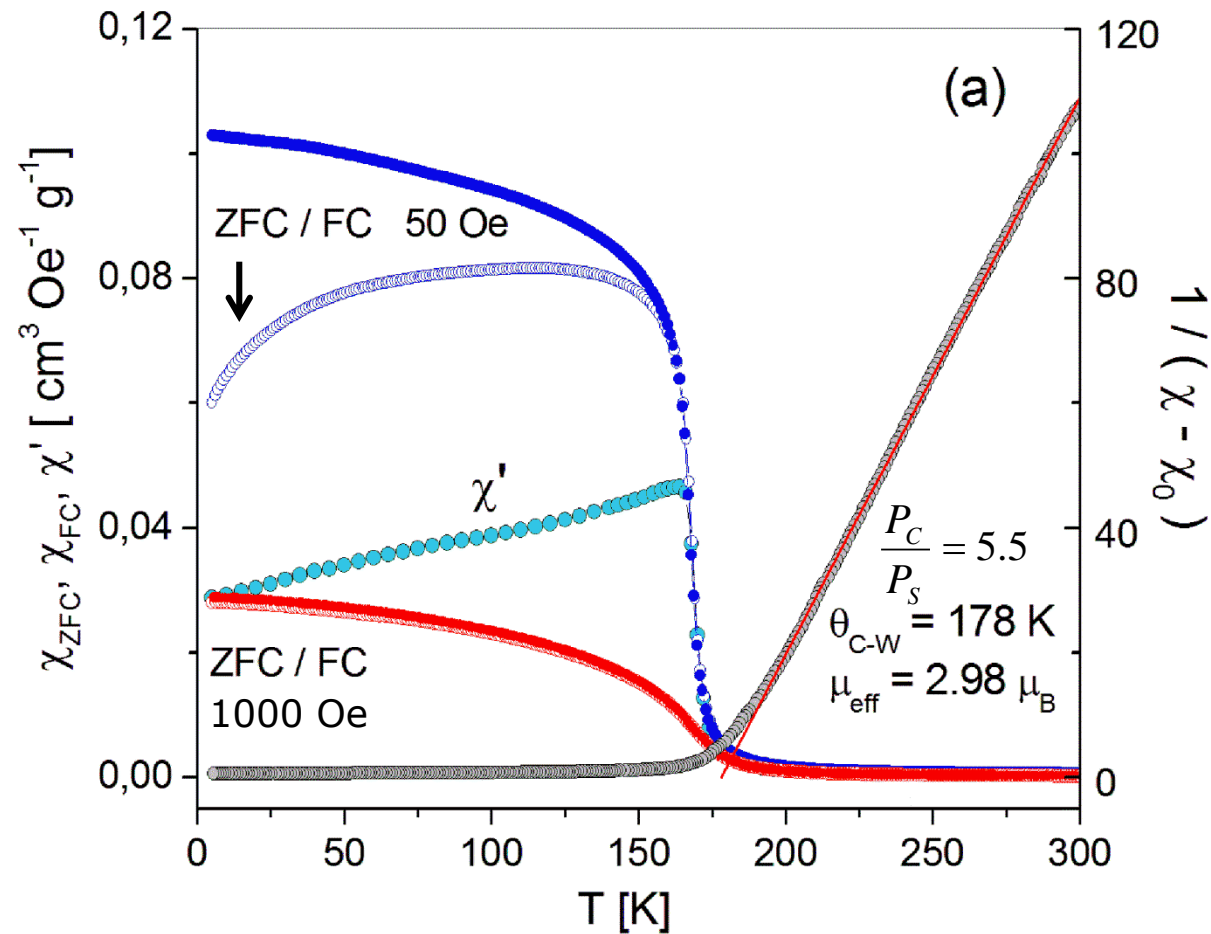


RESULTS: σ -FeV



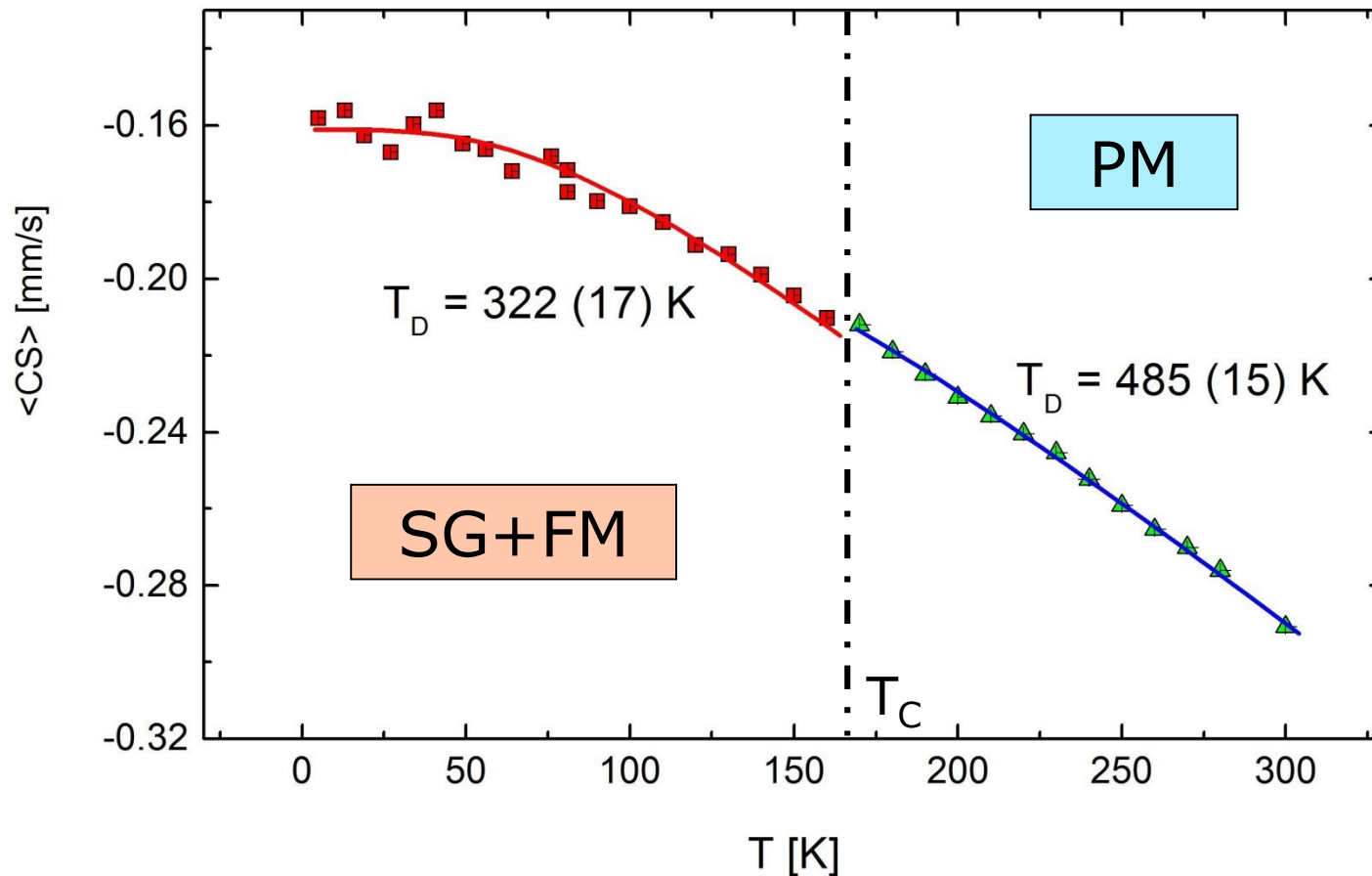
RESULTS: σ -FeV

$x_V=40$ at%

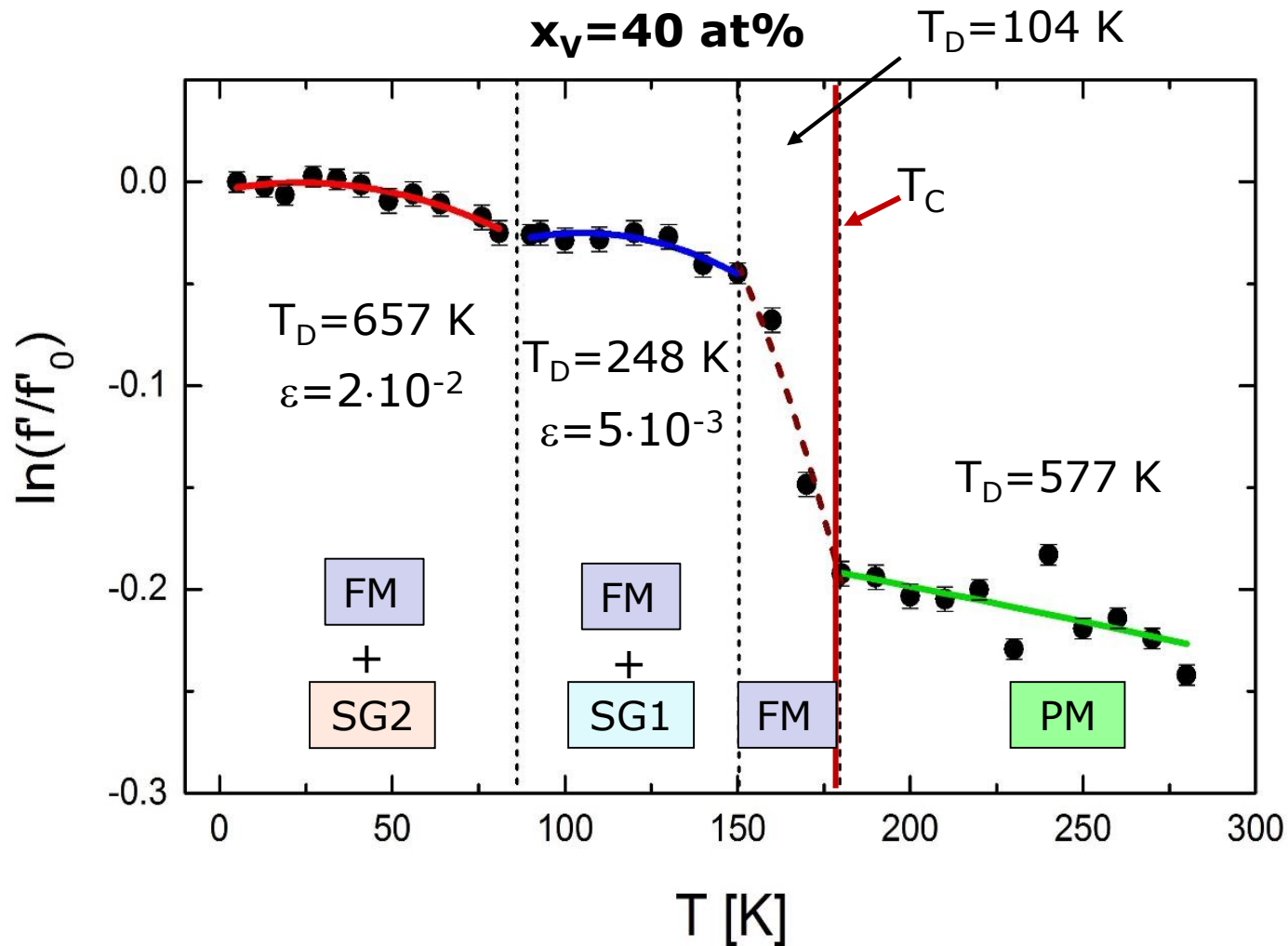


RESULTS: σ -FeV

◆ Debye temperature, T_D

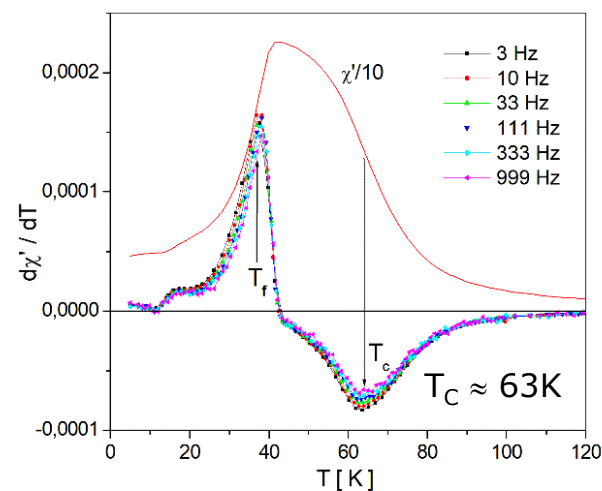
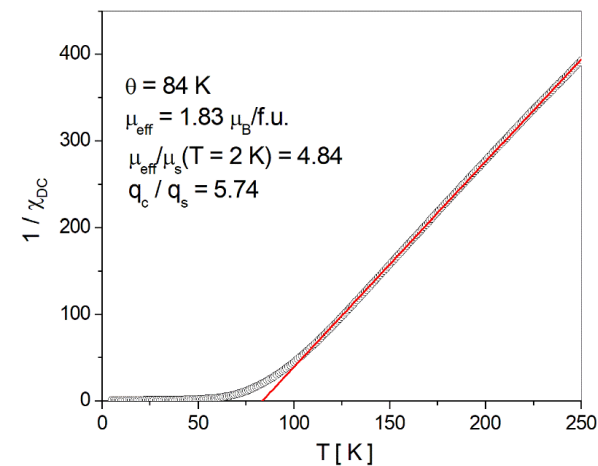
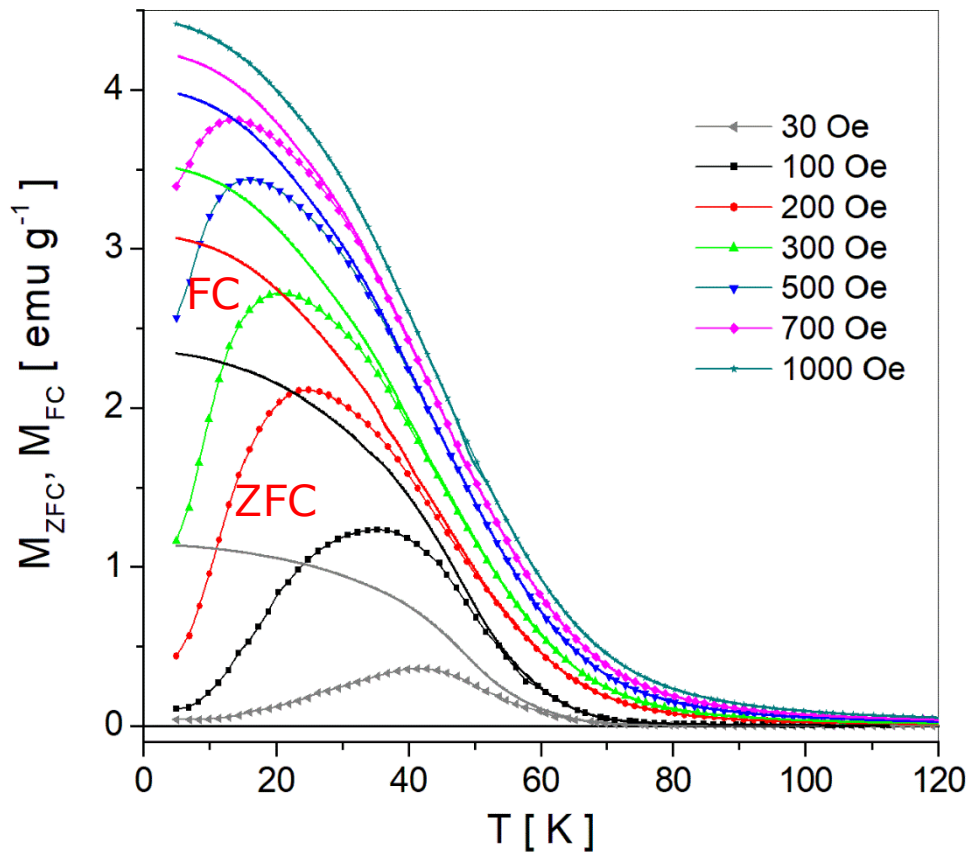


RESULTS: σ -FeV



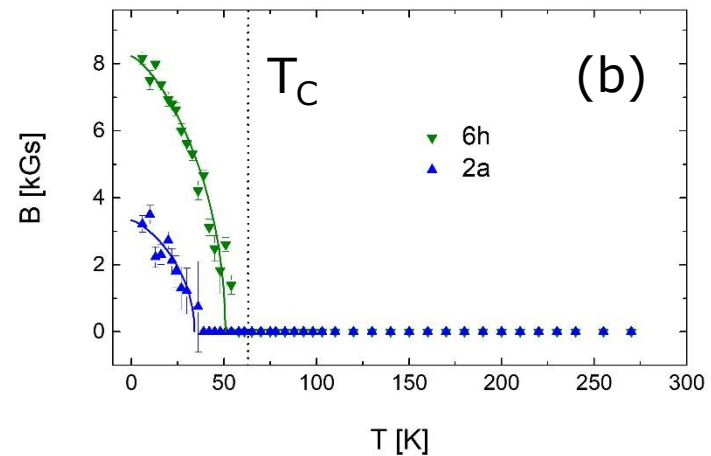
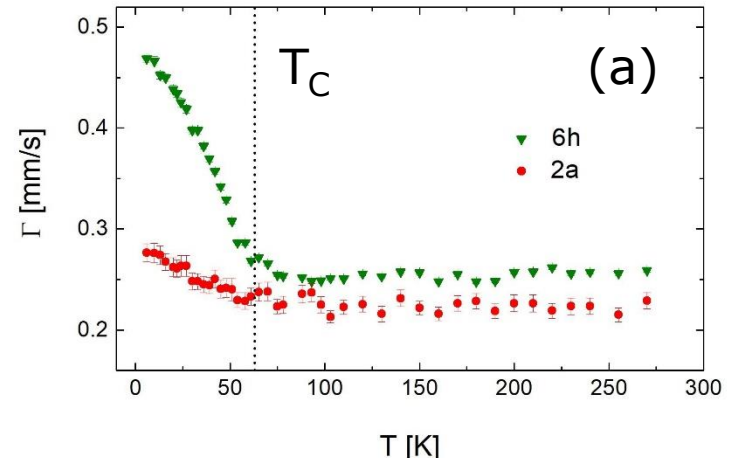
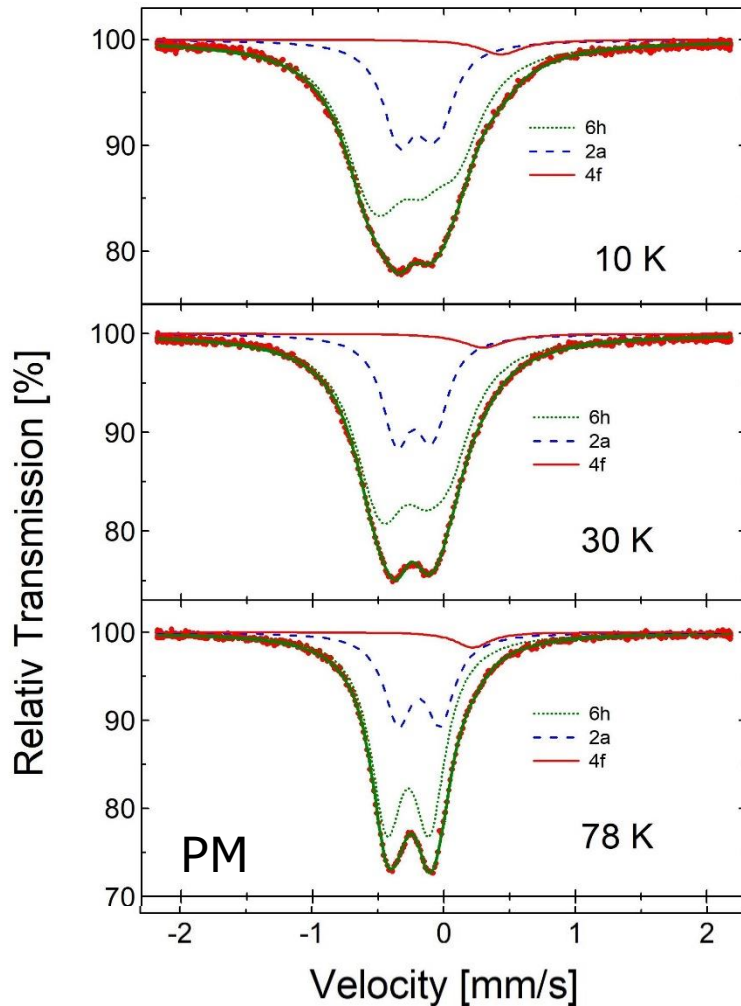
RESULTS: λ -Nb_{0.975}Fe_{2.025}

◆ DC and AC magnetic susceptibilities



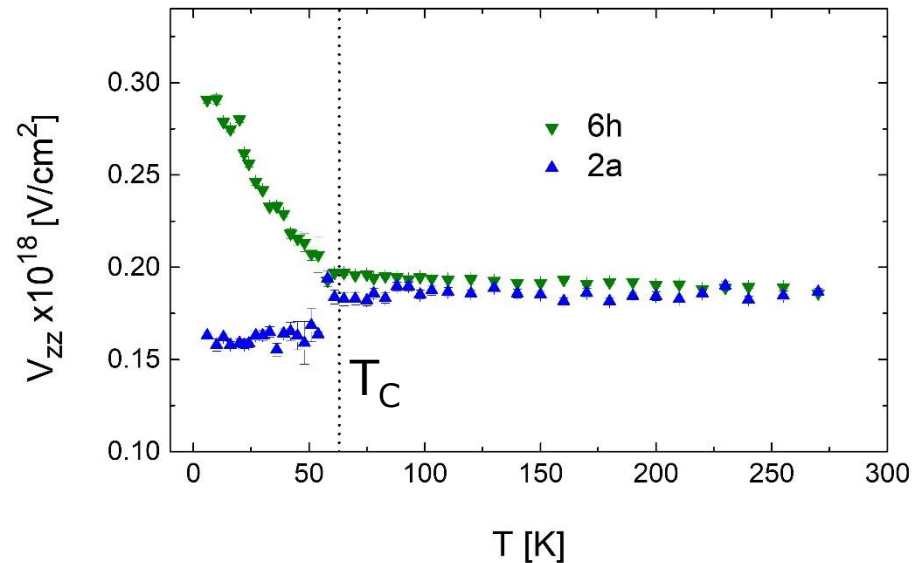
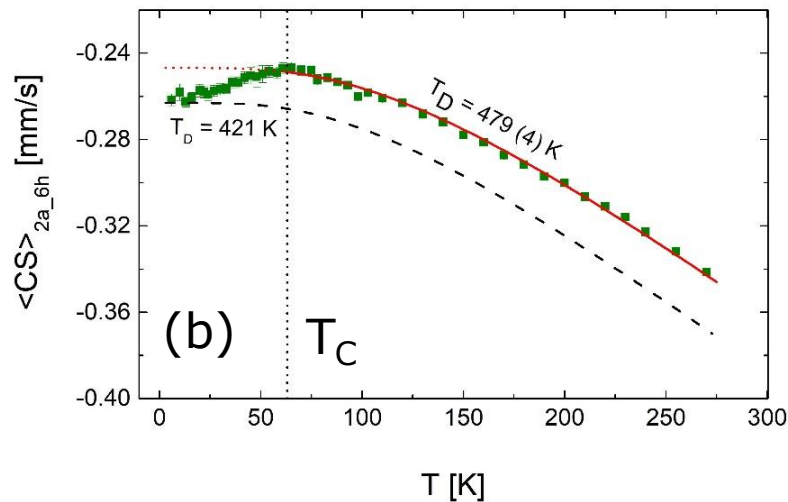
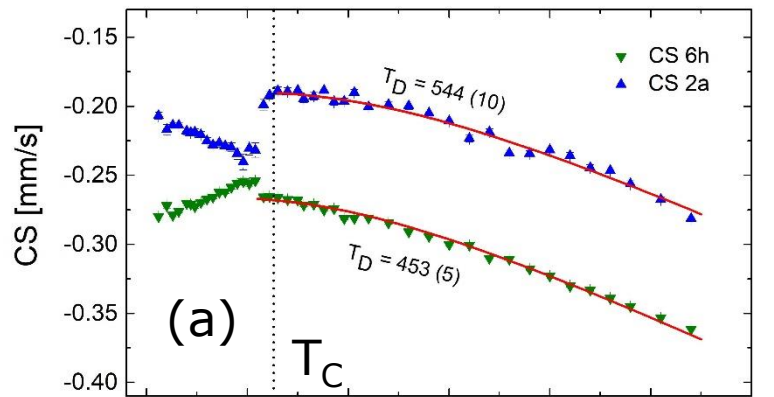
RESULTS: λ -Nb_{0.975}Fe_{2.025}

◆ Mössbauer measurements

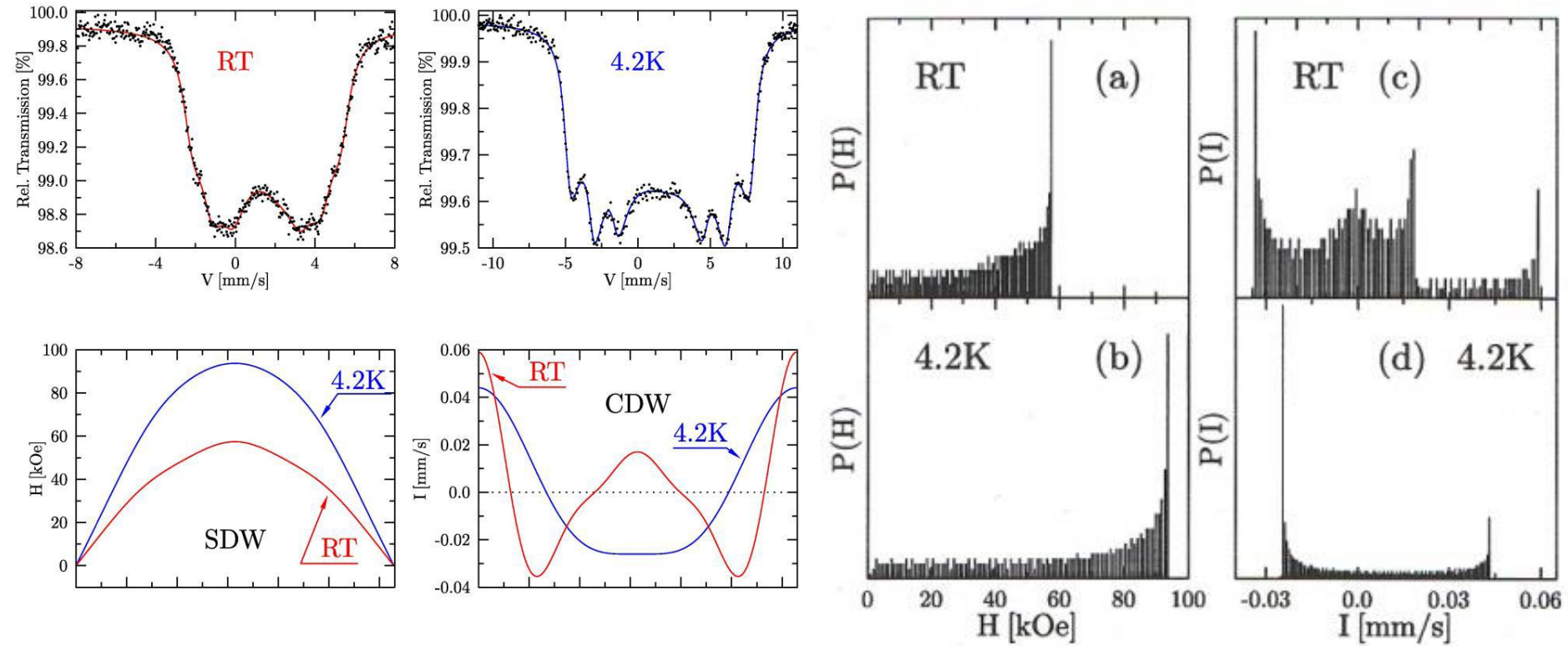


RESULTS: λ -Nb_{0.975}Fe_{2.025}

◆ Mössbauer measurements



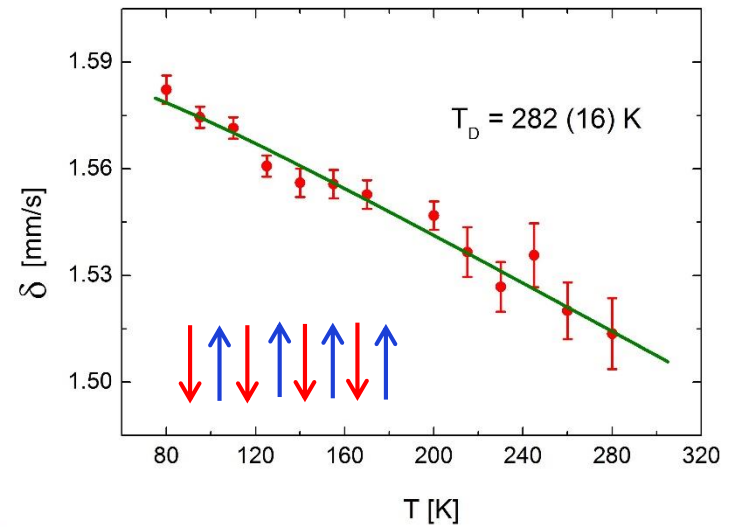
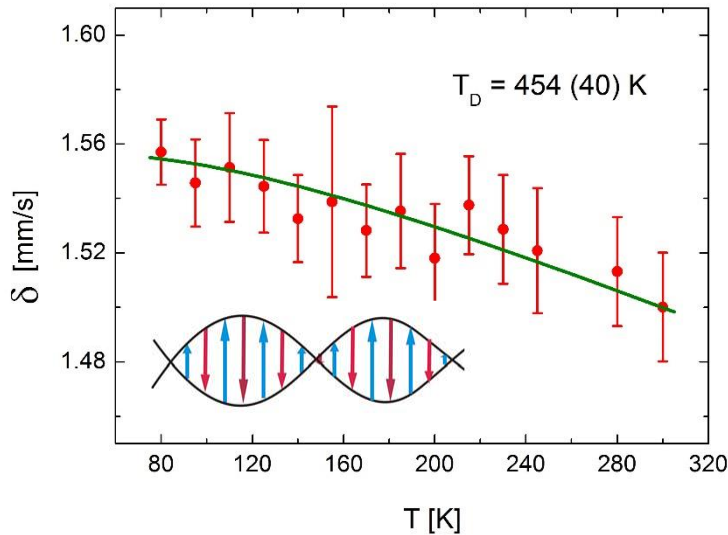
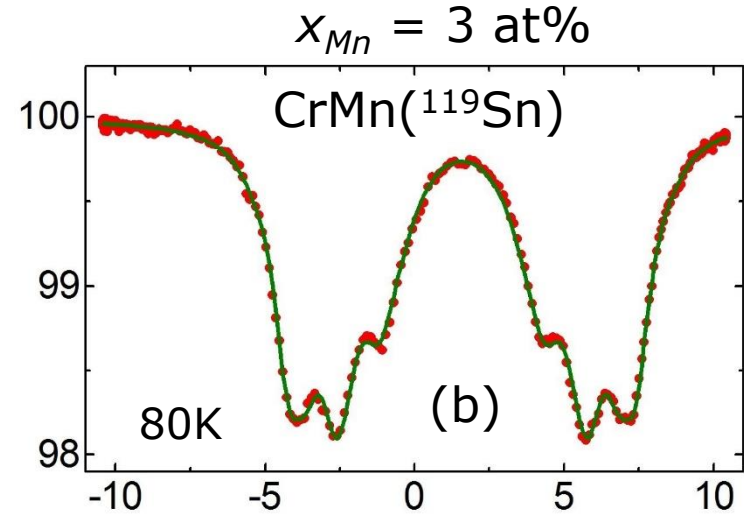
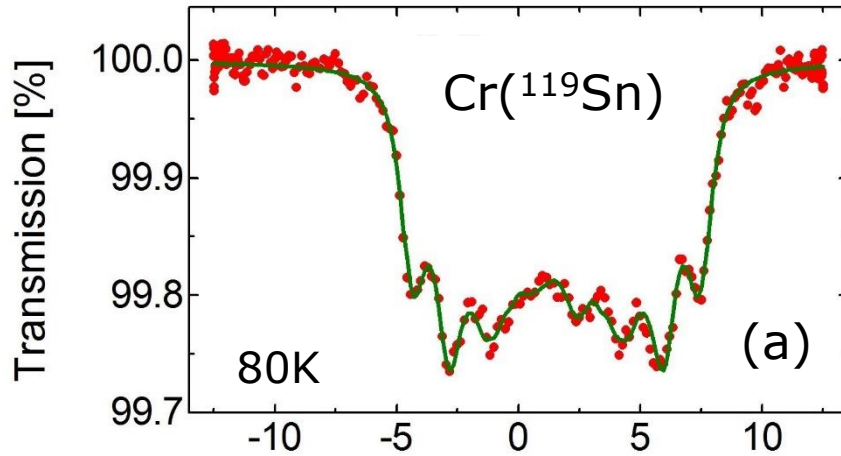
S.C.-CHROMIUM DOPED WITH ^{119}Sn



- Determination of H_3 : **2.6%** at 4.2K and **1.4%** at 295 K (**2.1%** from ND at 144K – Tsunoda 1985)

RESULTS: CHROMIUM

◆ ^{119}Sn Mössbauer measurements

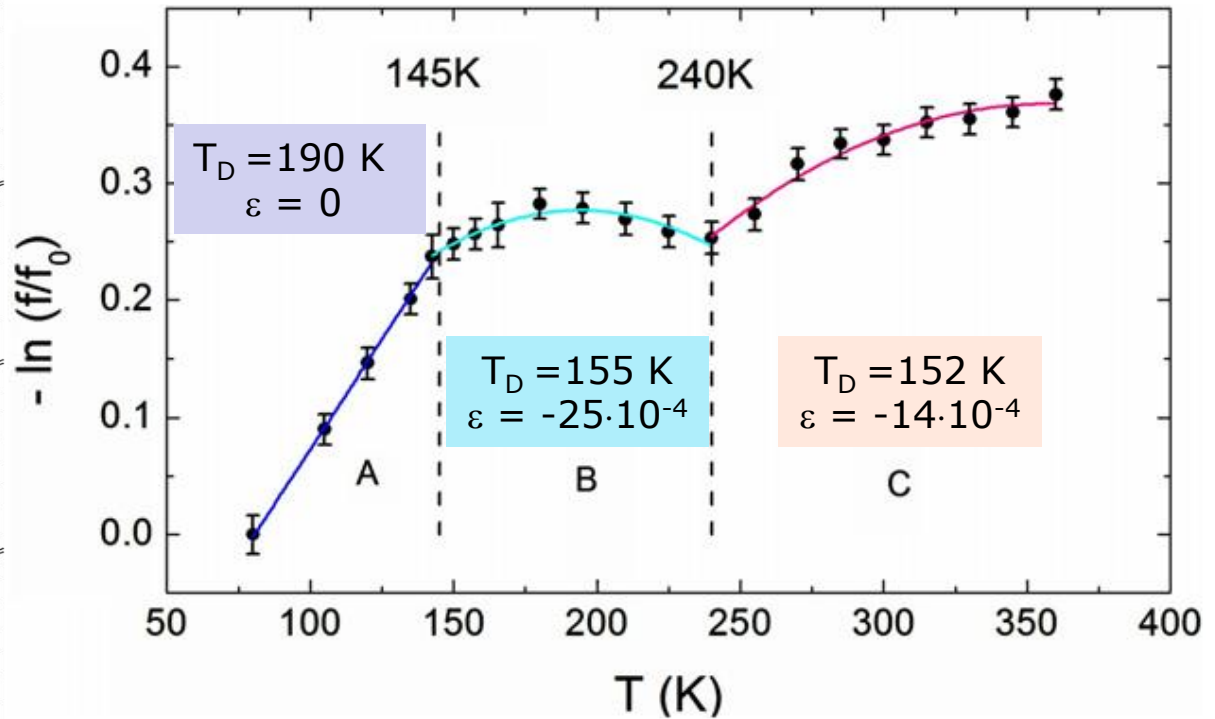
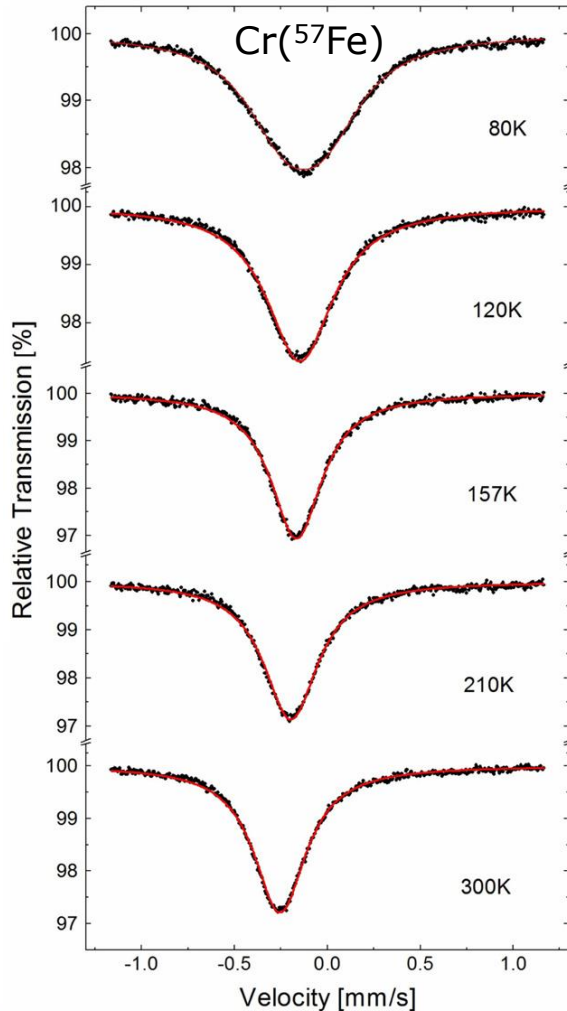




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RESULTS: CHROMIUM

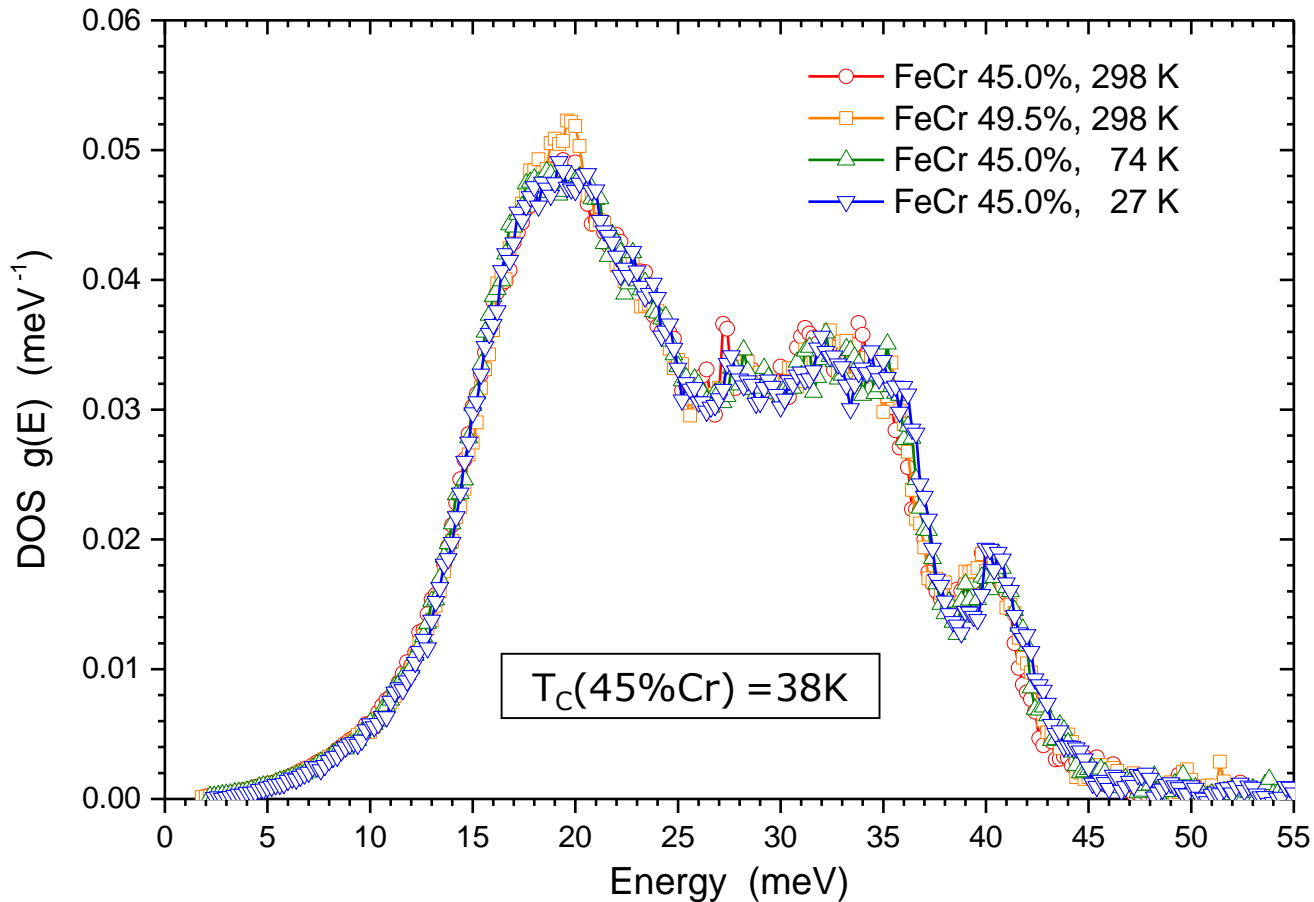
◆ ⁵⁷Fe Mössbauer measurements



$$-\ln f / f_0 = \ln f_0 - \frac{6E_R T}{T_D^2} (1 + \epsilon T)$$

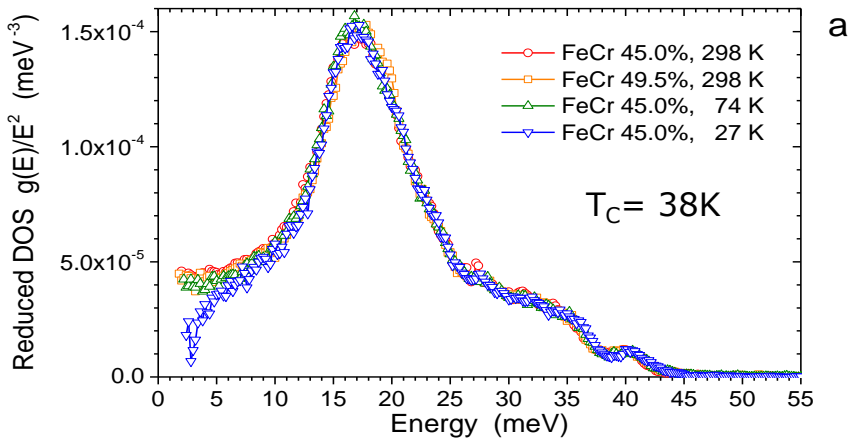
NIS RESULTS: σ -FeCr

◆ Fe-PDOS for σ -FeCr



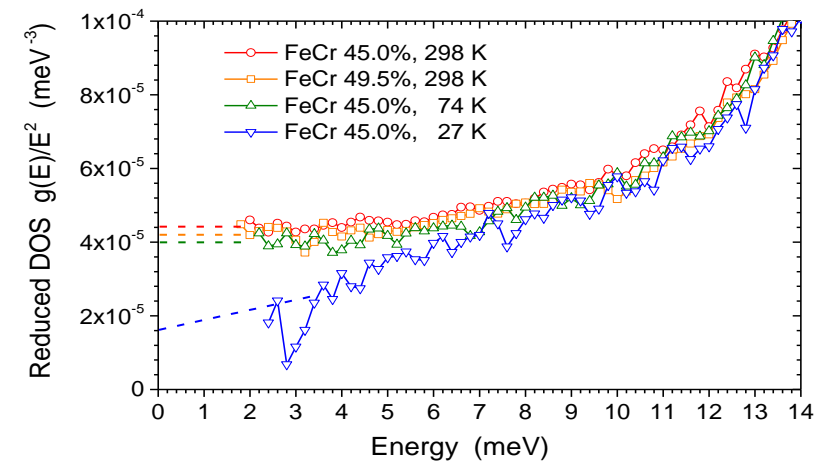
NIS RESULTS: σ -FeCr

◆ Effect of magnetism on sound velocity, $\langle v \rangle$



a

$$\lim_{E \rightarrow 0} \frac{g(E)}{E^2} = \frac{m_R}{\langle m \rangle} \frac{1}{2 \pi^2 \hbar^3 n \langle v \rangle^3}$$



b

x [at. % Cr]	T [K]	$g(E)/E^2$ [meV^{-3}]	$\langle v \rangle$ [km/s]
45	298(1)	$4.4(2) \times 10^{-5}$	3.68(7)
45	74.0(5)	$4.0(2) \times 10^{-5}$	3.79(7)
45	27.0(8)	$1.6(4) \times 10^{-5}$	5.1(4)
49.5	298(1)	$4.2(2) \times 10^{-5}$	3.75(7)

$$\Delta \langle v \rangle / v = 36\% (!)$$

CONCLUSIONS

Itinerant magnetism and external magnetic field strongly affect lattice dynamics:

(1) Deviations from the Debye model are observed below T_C in σ and λ Frank-Kasper phases viz.:

(a) Average squared velocity of vibrations (kinetic energy) increases.

(b) Average squared amplitude of vibrations decreases.

(c) Strong unharmonicity exists in the SG state.

(2) Significant differences revealed by ^{119}Sn and ^{57}Fe probe atoms in Cr viz.:

(a) T_D -values revealed by ^{119}Sn are ~ 2 -fold higher (Fe atoms are weakly coupled to SDWs).

(b) T_D -values obtained from ^{119}Sn spectra are significantly larger for ISDW than for CSDW (AF).

(3) Strong ($\sim 36\%$) increase in the average sound velocity was revealed for the $\sigma\text{-Fe}_{55}\text{Cr}_{45}$ compound in the magnetic state.



COLLABORATORS



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THANK YOU!

