

Struktura elektronowa i dynamika sieci czystego i zdefektowanego CoO

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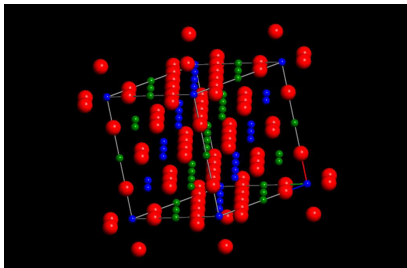
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Outline

- 1 Introduction
 - structure, electronic and magnetic properties of CoO
- 2 Methodology
- 3 Results for defect-free CoO
- 4 Phonons (direct method)
- 5 Cobalt-deficient CoO
 - electronic structure
 - lattice dynamics
- 6 Fe-doped CoO
 - lattice dynamics
 - charge and spin states of Fe in CoO and vacancy-defected CoO
 - electronic structure

CoO structure



High temperature structure

- Paramagnetic ($Fm\bar{3}m$)
- $a_{exp} = 4.26 \text{ \AA}$

Low temperature structure

- distorted NaCl structure ($R\bar{3}m$) below $T_N = 293 \text{ K}$
- rhombohedral distortion along $\langle 111 \rangle$, $0.2 - 0.3^\circ$
- 2nd kind of antiferromagnetic ordering, **AFII** structure

Electronic and magnetic properties of CoO

Experiment

- Insulator, $E_g = 2.5 - 2.8$ eV (experiment)
- $M_{total} = 3.8 - 3.98 \mu_B$

Theory (DFT)

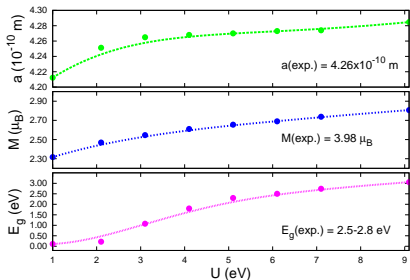
- Charge-transfer insulator
- **Strong on-site Coulomb interactions in 3d shell cannot be neglected** (strongly correlated electron system)
- DFT+U formalism required
- Interactions between correlated states - Hubbard potential U and the exchange interaction J

Calculations with +U formalism

Pseudopotential plane-wave method - VASP code

- spin-polarized DFT for AFII structure (64-atom supercell)
- Projector-augmented wave pseudopotentials (PAWs)
- Exchange-interaction: GGA+U
- Full relaxations of AFII structure
- $U = ?$, $J = ?$

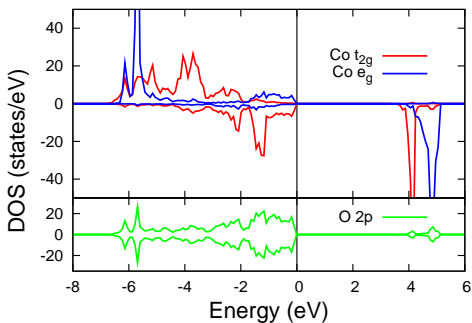
Energy gap, spin magnetic moment, lattice constant vs U



Results

- a - weak dependence upon U
- M_S changes by ca. 17%
- Underestimation of E_g for $U < 5$ eV
- E_g **vanishes** for $U = 1$ eV (GGA limit)

Defect-free CoO. Results for $U = 7.1$ eV, $J = 1$ eV



$U = 7.1$ eV, $J = 1$ eV

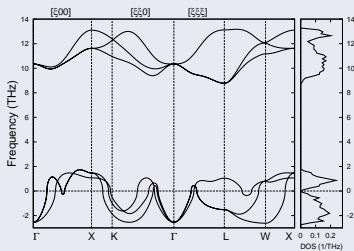
- $a = 4.27 \text{ \AA}$
- Rhombohedral distortion along $\langle 111 \rangle$ (0.3°)
space group $D_{3d}^5 (R\bar{3}m)$
- $E_g = 2.77$ eV
- $M_S = 2.74 \mu_B$

Method to calculate phonons

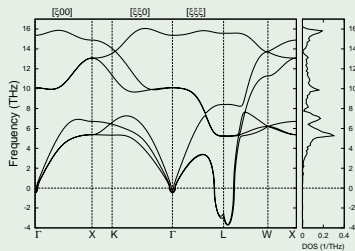
- Harmonic approximation
- Direct method - **PHONON** software by K. Parlinski
 - displace crystallographically nonequivalent atoms from their equilibrium positions
 - calculate Hellmann-Feynman forces $\mathbf{F}(\mathbf{n}, \mu) = \frac{-\delta E}{\delta \mathbf{R}(\mathbf{n}, \mu)}$
 $F_i(\mathbf{n}, \mu) = - \sum_{\mathbf{m}, \nu, j} \Phi_{ij}(\mathbf{n}, \mu, \mathbf{m}, \nu) U_j(\mathbf{m}, \nu)$
 - solve dynamical matrix $\mathbf{D}(\mathbf{k})$
 $\omega^2(\mathbf{k}, j) \mathbf{e}(\mathbf{k}, j) = \mathbf{D}(\mathbf{k}) \mathbf{e}(\mathbf{k}, j)$
↓
 - $\omega(\mathbf{k}, j)$ - phonon frequencies
 - $\mathbf{e}(\mathbf{k}, j)$ - polarization vectors of phonons

Phonon dispersion relations for $U = 0$ eV and $U = 3$ eV

$U_{\text{eff}} = 0$ eV



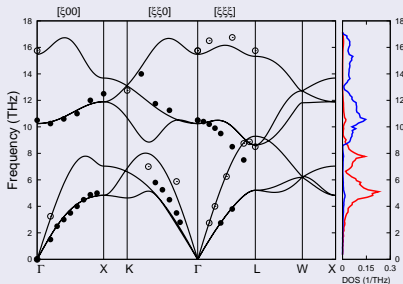
$U_{\text{eff}} = 2$ eV



- **imaginary frequencies** of acoustic modes \Rightarrow **instability** of such CoO structure
- significantly **underestimated HF forces** \Rightarrow **artificial mode softening**
- small U_{eff} \Rightarrow too low repulsion in 3d shell

Dispersion relations and phonon DOS for $U = 7 \text{ eV}$

$U = 7.1 \text{ eV}, J = 1 \text{ eV}$



Data for LO-TO splitting

- $\mathbf{D}(\mathbf{k}) = \mathbf{D}_0(\mathbf{k}) + D_N(\epsilon_\infty, \mathbf{Z}^*, \dots)$
- high-frequency dielectric constant
 $\epsilon_\infty = 5.3^{[1]}$
- Born effective charges
 $|\mathbf{Z}^*| = 2.06$

Experimental data from neutron scattering ($T = 110 \text{ K}$)

[1] J. Sakurai, W.J.L. Buyers, R.A. Cowley, and G. Dolling, Phys. Rev. 167, 510 (1968)

Comparison with experiment

Experiment vs theory

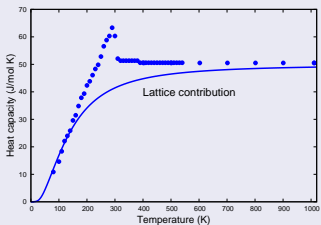
Γ -point frequencies (THz)	Neutron scattering ^[1]	Infrared spectroscopy ^[2]	Theory
ω_{TO}	10.50	10.40-10.50	10.25
ω_{LO}	15.75	16.30-16.40	15.73

Experimental data

- [1] J. Sakurai, W.J.L. Buyers, R.A. Cowley, and G. Dolling, Phys. Rev. 167, 510 (1968)
[2] J.P. Gielisse, J.N. Plendl, L.C. Mansur, R. Marshall, S.S. Mitra, R. Mikolajewicz, and A. Smakula, J. Appl. Phys. 36 2426 (1965)

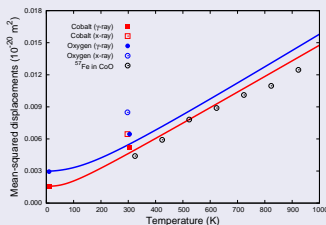
Heat capacity and Debye-Waller factors

Heat capacity



- magnetic contribution below T_N
- Dulong-Petit law @ HT

Debye-Waller factors



- calculated $\Theta_D = 500$ K
- Mössbauer $\Rightarrow \Theta_D = 440$ K

[3] E.G. King and A.U. Christensen, U.S. Bur.Mines. Tech. Paper 80, 1800 (1956); E.G. King, *ibid.* 80, 2399 (1956)

[4] W. Jauch and M. Reehuis, *PRB* 65, 125111 (2002)

[5] S. Sasaki, F. Fujino, and K. Takeuchi, *Proc. Jpn. Acad. B* 55, 43 (1979)

[6] K. Ruebenbauer and U.D. Wdowik, *J. Phys. Chem. Solids* 65, 1785 (2004)

Is CoO a stoichiometric material?

Native defects in CoO - cationic vacancies

- Co deficiency in 'almost stoichiometric' samples: 0.1-3%
- uncharged, singly and doubly charged vacancies
- nonstoichiometry depends on temperature and oxygen partial pressure

How to simulate point defects (vacancies, impurities)

- supercell approach
- remove atoms \Rightarrow vacancies
- replace host atoms by different kind of atoms \Rightarrow impurities

Modeling of non-stoichiometric CoO

Co_{0.97}O

- Co @ $(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$ removed from 64-atom SC



- CoO with 3% vacancies

Co_{0.94}O

- Co @ $(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$ and $(\frac{1}{2}, \frac{1}{2}, 0)$ removed from 64-atom SC



- CoO with 6% vacancies

Atomic relaxation in defected systems

- oxygens surrounding vacancies displace outward vacancy site by 0.12 Å
- initial Co-O distance (2.15 Å) changes by ca. 0.01 Å

Trivalent cations in CoO

Pure CoO

- $M_S = 2.74\mu_B$
- valence charges $q_{Co} = +1.33e$, $q_O = -1.33e$
- $Co^{2+}-O$ 2.15 Å

Co_{0.97}O

- $M_S = 3.15\mu_B$
- $q_{Co} = +1.65e$
- $Co^{3+} - O$ 2.05 Å
- 2 Co^{3+} in SC

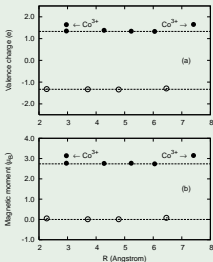
Co_{0.94}O

- $M_S = 3.16\mu_B$
- $q_{Co} = +1.68e$
- $Co^{3+} - O$ 2.05 Å
- 4 Co^{3+} in SC

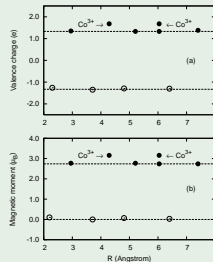
Electronic structure of CoO defected by cationic vacancies

Location of trivalent cations

$\text{Co}_{0.97}\text{O}$



$\text{Co}_{0.94}\text{O}$



Co^{3+} distance from vacancy

● 2.96 Å 7.41 Å

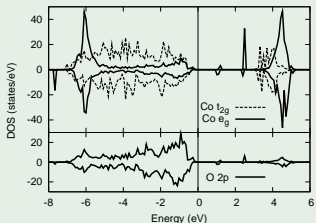
Co^{3+} distance from vacancy

● 4.29 Å 6.04 Å

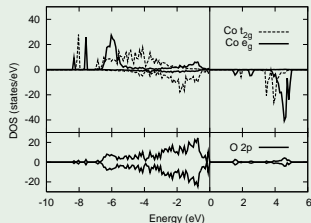
Electronic structure of CoO defected by cationic vacancies

Electronic structure of vacancy-defected CoO

Co_{0.97}O



Co_{0.94}O



- charge transfer from Co to O (via s,p states)
- $\text{Co}^{2+} \Rightarrow \text{Co}^{3+} + e^{-}$
- 2 holes associated with vacancy are compensated by 2 Co^{3+}

acceptor states in Co_{0.97}O

- 1 eV above VBM

acceptor states in Co_{0.94}O

- 1.5 eV above VBM

Description of phonons within SC approach

CoO

- primitive UC
 $N = 2 \Rightarrow 6$ branches

CoO as 64 atom SC

- $N_S = 64 \Rightarrow 192$ branches ?

Co_{0.97}O

- SC - already primitive UC
 $N_S = 63 \Rightarrow 189$ branches ?

- dimensions of $\mathbf{D}(\mathbf{k})$ increases to $3N_S$
- number of phonon dispersion curves increases to $3N_S$
- size of BZ conjugated with SC shrinks
- selection of a different kind of unit cell
↓
number of phonon dispersion curves is blown up.

Phonon form factor and *filter*

Phonon form factor

$$F^{(p)}(\mathbf{k}, j) = \frac{1}{k^2} \left| \sum_{\mu} \frac{\mathbf{k} \cdot \mathbf{e}(\mathbf{k}, j; \mu)}{\sqrt{M_{\mu}}} \right|^2$$

$$\int_{\Omega} d\Omega F^{(p)}(\mathbf{k}, j) = \frac{1}{3} F^{(s)}(\mathbf{k}, j)$$

Filter

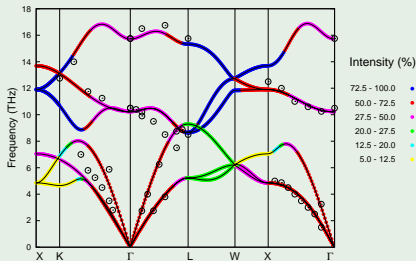
$$F^{(s)}(\mathbf{k}, j) = \left| \sum_{\mu} \frac{\mathbf{e}(\mathbf{k}, j; \mu)}{\sqrt{M_{\mu}}} \right|^2$$

Fake phonon modes

$$F^{(p)}(\mathbf{k}, j) = 0$$

Application of filter to stoichiometric CoO

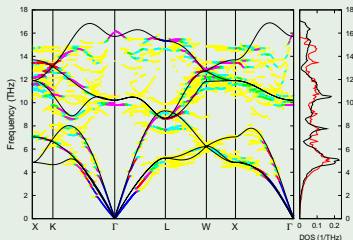
Intensities of modes for CoO



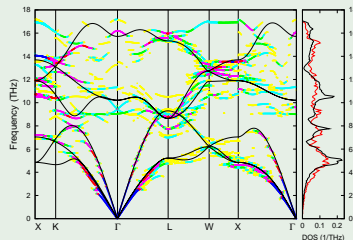
experimental data
close to branches with
intensities > 30%

Application of filter to nonstoichiometric CoO

$\text{Co}_{0.97}\text{O}$



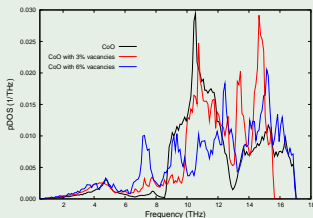
$\text{Co}_{0.94}\text{O}$



- perturbed phonons with wavelength \sim size of region disturbed by vacancy
- missing Co \Rightarrow additional O vibrations (new modes)
- acoustic branches at small \mathbf{k} not affected by vacancies
 \downarrow
 long wavelength phonons insensitive to point defects

Oxygens surrounding vacancies

Partial DOS



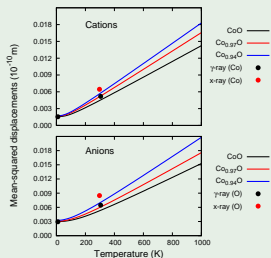
- vacancies affect the highest frequency LO modes
- no change in low-frequency acoustic region

Γ -point frequencies

frequency (THz)	CoO	Co _{0.97} O	Co _{0.94} O
ω_{TO}	10.25	9.81	9.61
ω_{LO}	15.73	15.87	16.08

Mean-squared displacements vs T

MSD for Co and O



Co and O at low T

- 5% larger MSD than in stoichiometric CoO
- negligible difference between Co_{0.97}O and Co_{0.94}O

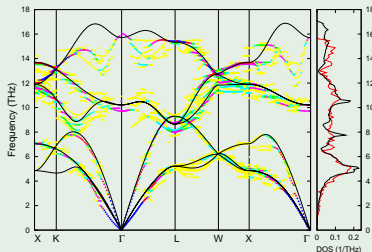
Co and O above RT

	Co	O
Co _{0.97} O	13%	19%
Co _{0.94} O	22%	23%

Lattice dynamics of Fe-doped CoO

Dispersion curves.

$$U_{\text{Fe}} = U_{\text{Co}} = 7.1 \text{ eV}$$



- localized modes
- mass defect negligible
- change in on-site force constant at Fe site
- at Co site $\Phi = 10.013 \text{ (eV/\text{Å}^2)}$ const. vs U_{Fe}

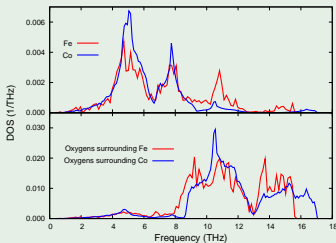
Force constant at Fe site

U_{Fe} (eV)	5.1	6.1	7.1
Φ (eV/Å ²)	12.264	12.787	13.313

Dynamics of Fe impurity

Partial phonon DOS

$$U_{\text{Fe}} = U_{\text{Co}} = 7.1 \text{ eV}$$



splitting of ω_{TO}

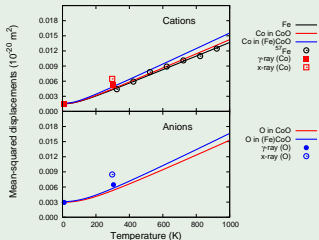
- modes corresponding to:
 - oxygens vibrating around Co
 - $\omega_{\text{TO}} = 10.51 \text{ THz}$
 - const. vs U_{Fe}
 - oxygens vibrating around Fe

oxygens neighboring Fe

U_{Fe} (eV)	5.1	6.1	7.1
ω_{TO} (THz)	9.67	9.68	9.72

Debye-Waller factors in Fe-doped CoO

Vibrational amplitudes



- $MSD_{Fe} < MSD_{Co} < MSD_O$
- 5% increase in MSD_{Fe} with decreasing U_{Fe}

Low T (10 K)

- $MSD_{Co} > MSD_{Fe}$ by 7% mass + force constant defect
- MSD_{Co}, MSD_O in $Co(Fe)O$ are 4% higher than respective $MSDs$ in CoO (const. vs U_{Fe})

Above RT ($U_{Fe} = 7.1 \text{ eV}$)

- MSD_{Fe} slope calc. = exp. $Co(^{57}Fe)O$

	Co(Fe)O	Co(^{57}Fe)O	CoO
Θ_D (K)	440	440	500

Valence and spin states of Fe in CoO and CoO_{0.97}O

Experiment - Mössbauer spectroscopy

- 2 singlets @ RT
 - ferrous line Fe²⁺
 - ferric line Fe³⁺
 - vicinity of T_N = 293 K
 - magnetically split component due to Fe²⁺
- T = 78 K magnetically split Fe²⁺ and Fe³⁺
G. K. Wertheim, Phys. Rev. 124, 764 (1961)

Method

FP-(L)APW+lo (WIEN2k code)

Full-potential(linearized) augmented plane-wave plus local orbitals

↓

Isomer shift and EFG on Fe in Co(Fe)O and Co(Fe,V)O

Charge and spin states

- different Fe-V complexes in CoO considered
- negligible changes vs U_{Fe}
- $\alpha = -0.291 \text{ a.u.}^3 \text{ mms}^{-1}$
 $Q = +0.17 \text{ b}$

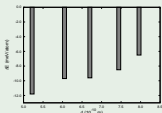
U.D. Wdowik and K. Ruebenbauer, PRB 76, 155118 (2007)

Results

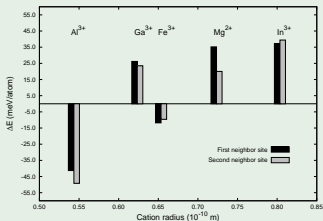
	Co(Fe)O	Co _{0.97} (Fe)O	Exp.[6]
$M_{\text{Co}} (\mu_B)$	2.74	2.74 Co ²⁺ 3.13 Co ³⁺	
$M_{\text{Fe}} (\mu_B)$	3.67	4.27	
IS (mm/s)	-1.031	-0.371	-1.1245(8) Fe ²⁺ -0.37(5) Fe ³⁺
EFG (mm/s)	0.27	0.28	0 0.3-0.4 mm/s linewidth
η	0.03	0.07	0

Site preferences

Fe-V complex in CoO



Trivalent and divalent impurities in vacancy-defected CoO



magnetic impurities

- Fe^{3+} in 1st n.s.
- Co^{3+} in 2nd n.s.
exception: Fe^{3+} in 2nd n.s.

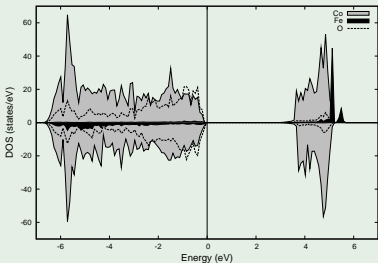
non-magnetic impurities

- 'small' trivalent cations in 2nd n.s.
- 'large' trivalent cations in 1st n.s.
- divalent cations in 2nd n.s.

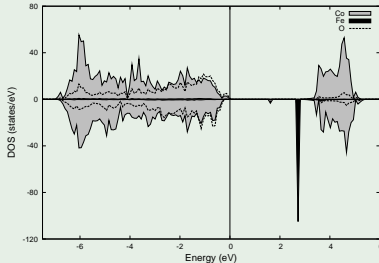
Electronic structure of Co(Fe)O and Co(Fe,V)O

Density of states for Co(Fe)O and $\text{Co}_{0.97}(\text{Fe})\text{O}$

DOS of Fe-doped CoO



DOS of Fe-doped $\text{Co}_{0.97}\text{O}$



- Co^{3+} and Fe^{3+} states inside gap

Summary and conclusions

- 1 DFT+U can predict correct ground states of CoO
- 2 Trivalent Co are found in vacancy-defected CoO
- 3 Filter allows to present phonon-dispersion curves to be more close to the dispersion relations of a real defected sample
- 4 Point defects influence mainly optical phonon region. Long-wavelength acoustic phonons are practically not affected by defects, i.e., small concentration of defects does not disturb those crystal properties which are due to the low-frequency acoustic phonons
- 5 Average MSDs of ions increase with increasing vacancy concentration (decreased intensity of scattered radiation)
- 6 Differences in the vibrational dynamics of a dopant and host atoms arise from the difference in their force constants
- 7 Divalent Fe is found in the host CoO lattice undisturbed by cobalt vacancies
- 8 Trivalent Fe is found in the host CoO lattice decorated with cobalt vacancies
- 9 Details can be found in PRB 75, 104306 (2007); PRB 77, 115110 (2008); PRB 78, 224114; J.Phys.:Condens. Matter 21, 125601 (2009)