

CRACOVIAN THEORETICAL RESULTS FOR ULTRAPERIPHERAL HEAVY-ION COLLISIONS

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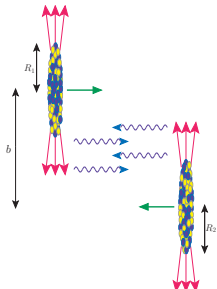
EPA

PHOTON-PHOTON SCATTERING

FOUR-LEPTON PRODUCTION

PROTON-ANTIPROTON PRODUCTION

CONCLUSION

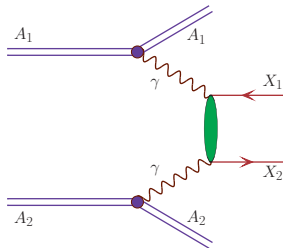


ULTRAPERIPHERAL COLLISIONS

$$b > R_{min} = R_1 + R_2$$

1. M. K-G, P. Lebiedowicz, A. Szczurek, Light-by-light scattering in ultraperipheral Pb-Pb collisions at energies available at the CERN Large Hadron Collider, Phys. Rev. **C93** (2016) 044907,
2. M. K-G, W. Schäfer, A. Szczurek, Two-gluon exchange contribution to elastic $\gamma\gamma \rightarrow \gamma\gamma$ scattering and production of two-photons in ultraperipheral ultrarelativistic heavy ion and proton-proton collisions, Phys. Lett. **B761** (2016) 399,
3. M. K-G, A. Szczurek, Double scattering production of two positron–electron pairs in ultraperipheral heavy-ion collisions, Phys. Lett. **B763** (2016) 416,
4. A. van Hameren, M. K-G, A. Szczurek, From the Single- and double-scattering production of four muons in ultraperipheral PbPb collisions at the Large Hadron Collider, Phys. Lett. **B776** (2018) 84,
5. M. K-G, P. Lebiedowicz, O. Nachtmann, A. Szczurek, From the $\gamma\gamma \rightarrow p\bar{p}$ reaction to the production of $p\bar{p}$ pairs in ultraperipheral ultrarelativistic heavy-ion collisions at the LHC, Phys. Rev. **D96** (2017) 094029.

$\gamma\gamma$ fusion



✓ $\rho^0, J/\psi$

✓ $\rho^0\rho^0, J/\psi J/\psi$

✓ $\pi^+\pi^-, \pi^0\pi^0$

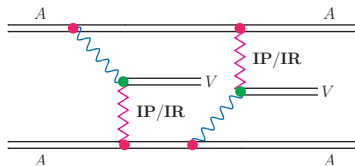
✓ $c\bar{c}, b\bar{b}$

✓ $e^+e^-, \mu^+\mu^-$

✓ $\gamma\gamma$

✓ $p\bar{p}$

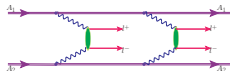
Photoproduction



✓ $\pi^+\pi^-\pi^+\pi^-$

✓ $e^+e^-e^+e^-$

✓ $\mu^+\mu^-\mu^+\mu^-$



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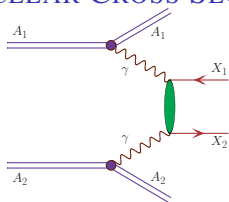
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ALICE, ATLAS, CMS, LHCb ($^{208}\text{Pb}+^{208}\text{Pb}$ @ $\sqrt{s_{NN}} = 2.76, 3.5, 5.02, 5.5$ TeV)

NUCLEAR CROSS SECTION

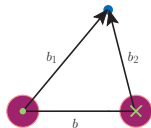


$$\sigma_{A_1 A_2 \rightarrow A_1 A_2 X_1 X_2} = \dots$$

$$\begin{aligned} \text{NAIVELY} \Rightarrow \dots &= \int d\omega_1 d\omega_2 n(\omega_1) n(\omega_2) \\ &\times \sigma_{\gamma\gamma \rightarrow X_1 X_2}(\omega_1, \omega_2) \end{aligned}$$

$$n(\omega) = \int_{R_{min}}^{\infty} 2\pi b db N(\omega, b)$$

$$\begin{aligned} \text{MORE CORRECTLY} \Rightarrow \dots &= \int N(\omega_1, \mathbf{b}_1) N(\omega_2, \mathbf{b}_2) S_{abs}^2(\mathbf{b}) \\ &\times \sigma_{\gamma\gamma \rightarrow X_1 X_2}(W_{\gamma\gamma}) \\ &\times d^2b d\bar{b}_x d\bar{b}_y \frac{W_{\gamma\gamma}}{2} dW_{\gamma\gamma} dY_{X_1 X_2} \end{aligned}$$



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PHOTON FLUX & FORM FACTOR

χ charge distribution in nucleus

$$N(\omega, b) = \frac{Z^2 \alpha_{em}}{\pi^2 \beta^2} \frac{1}{\omega} \frac{1}{b^2} \times \left| \int d\chi \chi^2 \frac{F\left(\frac{\chi^2 + u^2}{b^2}\right)}{\chi^2 + u^2} J_1(\chi) \right|^2$$

$$\beta = \frac{p}{E}, \gamma = \frac{1}{\sqrt{1-\beta^2}}, u = \frac{\omega b}{\gamma \beta}, \chi = k_{\perp} b$$

- ▶ point-like $F(\mathbf{q}^2) = 1$

$$N(\omega, b) = \frac{Z^2 \alpha_{em}}{\pi^2 \beta^2} \frac{1}{\omega} \frac{1}{b^2} \times u^2 \left[K_1^2(u) + \frac{1}{\gamma^2} K_0^2(u) \right]$$

- ▶ monopole $F(\mathbf{q}^2) = \frac{\Lambda^2}{\Lambda^2 + |\mathbf{q}|^2}$

$$\sqrt{\langle r^2 \rangle} = \sqrt{\frac{6}{\Lambda^2}} = 1 \text{ fm } A^{1/3}$$

FORM FACTOR

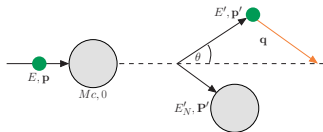


FIG.: Elastic scattering of electron-nucleus

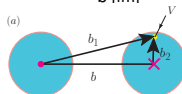
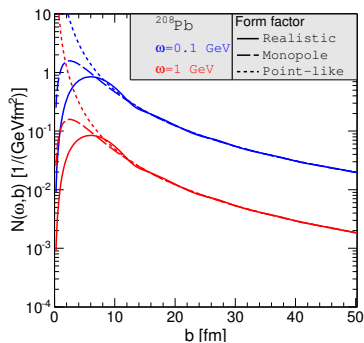
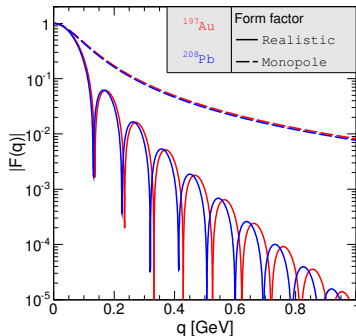
FORM FACTOR

&

PHOTON FLUX

- ▶ realistic charge distribution

$$F(\mathbf{q}^2) = \frac{4\pi}{|\mathbf{q}|} \int \rho(r) \sin(|\mathbf{q}| r) r dr$$



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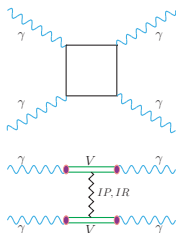
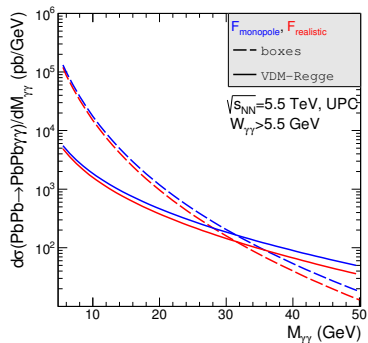
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AA \rightarrow AA $\gamma\gamma$ - FORM FACTOR

\Rightarrow realistic

\Rightarrow monopole



$\frac{\sigma_{\text{monopole}}}{\sigma_{\text{realistic}}} \nearrow$ for larger values of kinematic variables

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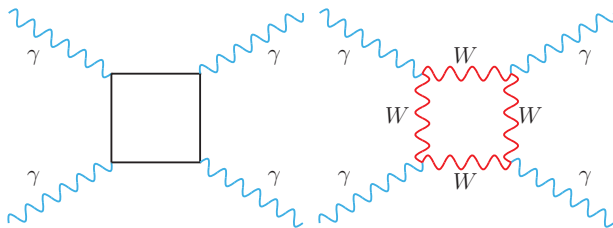
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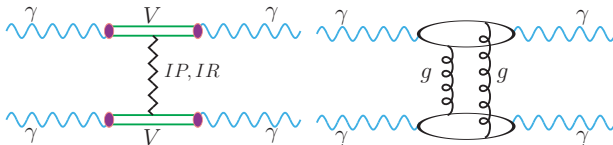
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$\gamma - \gamma$ ELASTIC SCATTERING

WELL-KNOWN



WE ADD



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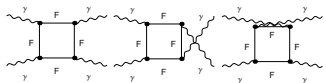
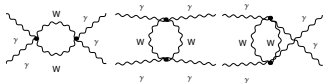
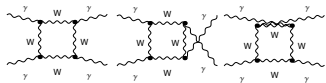
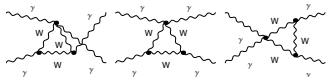
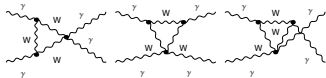
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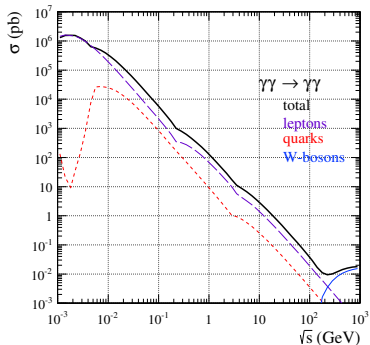
BOXES

$\gamma\gamma \rightarrow \gamma\gamma$



Fermionic box LO QED - FormCalc.

The one-loop W box diagram - LoopTools.



We have compared our results with:

- ▶ Jikia et al. (1993),
- ▶ Bern et al. (2001),
- ▶ Bardin et al. (2009).

Bern et al. consider QCD and QED corrections

(two-loop Feynman diagrams) to the one-loop

fermionic contributions in the ultrarelativistic limit

($\hat{s}, |\hat{t}|, |\hat{u}| \gg m_f^2$). The corrections are quite small

numerically.

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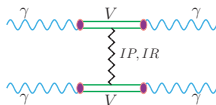
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VDM-REGGE CONTRIBUTION



$$\begin{aligned} \mathcal{A}_{\gamma\gamma\rightarrow\gamma\gamma}(s, t) &= \sum_i^3 \sum_j^3 C_{\gamma\rightarrow V_i}^2 \mathcal{A}_{V_i V_j \rightarrow V_i V_j} C_{\gamma\rightarrow V_j}^2 \\ &\approx \left(\sum_{i=1}^3 C_{\gamma\rightarrow V_i}^2 \right) \mathcal{A}_{VV\rightarrow VV}(s, t) \left(\sum_{j=1}^3 C_{\gamma\rightarrow V_j}^2 \right) \end{aligned}$$

$$i, j = \rho, \omega, \phi$$

$$\mathcal{A}_{VV\rightarrow VV}(s, t) = \mathcal{A}(s, t) \exp\left(\frac{B}{2}t\right)$$

$$\mathcal{A}(s, t) \approx s \left((1+i) C_{\mathbf{R}} \left(\frac{s}{s_0}\right)^{\alpha_{\mathbf{R}}(t)-1} + i C_{\mathbf{P}} \left(\frac{s}{s_0}\right)^{\alpha_{\mathbf{P}}(t)-1} \right)$$

- $C_{\gamma\rightarrow V_i}^2 = \frac{e}{f_{V_i}}$
- $C_{\mathbf{P}}, C_{\mathbf{R}}$ - Donnachie-Landshoff
- $\alpha_{\mathbf{R}}(t), \alpha_{\mathbf{P}}(t)$ - trajectories

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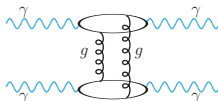
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2-GLUON EXCHANGE

16 diagrams \Rightarrow CRACOVIAN
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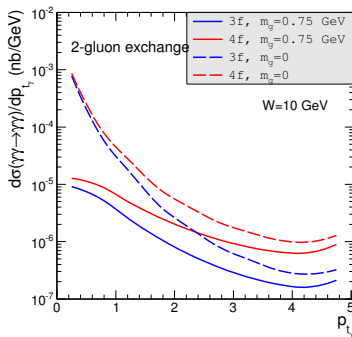
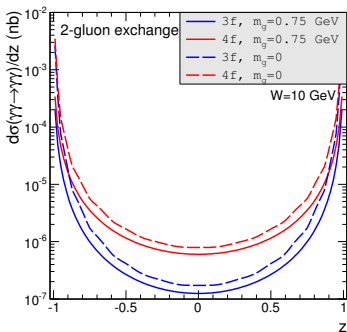
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$$z = \cos \theta ; \theta - \text{scattering } \angle$$

$$p_{t_\gamma} = p \sin \theta$$

 $3f = u, d, s$ $4f = u, d, s, c$

$m_U \approx 0.15 \text{ GeV}$

$m_D \approx 0.15 \text{ GeV}$

$m_S \approx 0.30 \text{ GeV}$

$m_C \approx 1.50 \text{ GeV}$

Significant effect of c quark inclusion at $z \approx 0$ (large p_{t_γ}) - interference

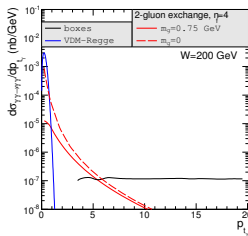
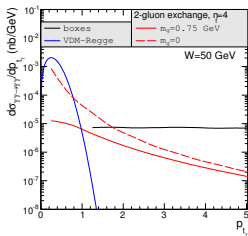
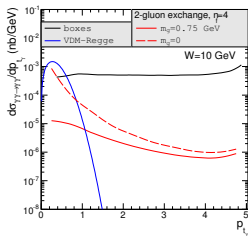
EXPERIMENTAL IDENTIFICATION OF PROCESSES?

- ✓ boxes
- ✓ VDM-Regge
- ✓ 2-gluon exchange

W = 10 GeV

W = 50 GeV

W = 200 GeV



$\gamma - \gamma$ Collider (the International e^+e^- Linear Collider) ?

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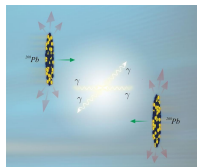
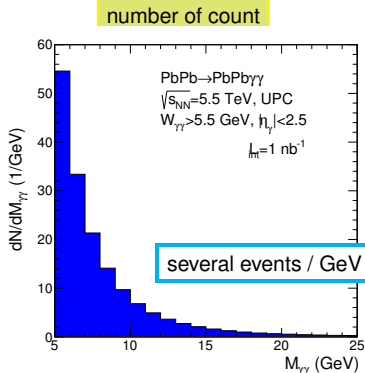
CONCLUSION

Photon collisions:

Photonic billiards might be the newest game!

www.eurekalert.org/pub_releases/

2016-05/thni-pcp051916.php



$\sigma(\text{PbPb}\rightarrow\text{PbPb}\gamma\gamma)$ [nb] at LHC ($\sqrt{s_{NN}} = 5.5$ TeV) and FCC ($\sqrt{s_{NN}} = 39$ TeV)

	cuts	boxes		VDM-Regge	
		$F_{realistic}$	$F_{monopole}$	$F_{realistic}$	$F_{monopole}$
L	$W_{\gamma\gamma} > 5$ GeV	306	349	31	36
	$W_{\gamma\gamma} > 5$ GeV, $p_{t,\gamma} > 2$ GeV	159	182	7E-9	8E-9
	$E_{\gamma} > 3$ GeV	16 692	18 400	17	18
H	$E_{\gamma} > 5$ GeV	4 800	5 450	9	611
	$E_{\gamma} > 3$ GeV, $ y_{\gamma} < 2.5$	183	210	8E-2	9E-2
C	$E_{\gamma} > 5$ GeV, $ y_{\gamma} < 2.5$	54	61	4E-4	7E-4
	$p_{t,\gamma} > 0.9$ GeV, $ y_{\gamma} < 0.7$ (ALICE cuts)	107			
	$p_{t,\gamma} > 5.5$ GeV, $ y_{\gamma} < 2.5$ (CMS cuts)	10			
F	$W_{\gamma\gamma} > 5$ GeV	6 169		882	
C	$E_{\gamma} > 3$ GeV	4 696 268		574	
C					

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AA \rightarrow AA $\gamma\gamma$ - THEORETICAL PREDICTIONS VS. EXPERIMENT

- \Rightarrow ATLAS Collaboration (M. Aaboud et al.),
 Evidence for light-by-light scattering in heavy-ion collisions with the ATLAS detector at the LHC,
 Nature Phys. **13** (2017) 852

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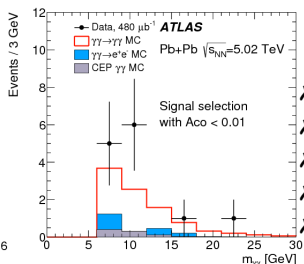
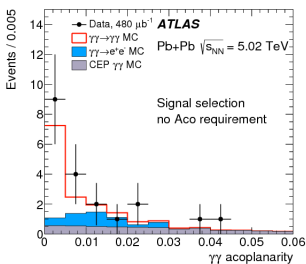
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- $\times p_{t\gamma} > 3$ GeV
- $\times |\eta_{\gamma}| < 2.4$
- $\times M_{\gamma\gamma} > 6$ GeV
- $\times p_{t\gamma\gamma} < 2$ GeV
- $\times \text{Aco} < 0.01$

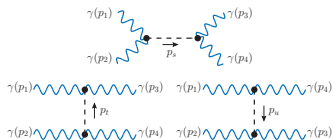
- ✓ $\gamma\gamma \rightarrow \gamma\gamma$ - using our calculations
- ✓ background:
 - ✓ $\gamma\gamma \rightarrow e^+e^-$
 - ✓ $gg \rightarrow \gamma\gamma$
 - ✓ $\gamma\gamma \rightarrow q\bar{q}$
- ✓ 13 events were observed

ATLAS $\Rightarrow \sigma = 70 \pm 20(\text{stat.}) \pm 17(\text{syst.}) \text{ nb}$

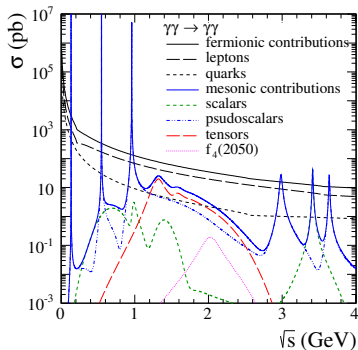
from ours model $\Rightarrow \sigma = 49 \pm 10 \text{ nb}$

PRL (2013)/(2016) $\Rightarrow \sigma = 45 \pm 9 \text{ nb}$

$M_{\gamma\gamma} < 5 \text{ GeV} \Rightarrow \text{MESON EXCHANGE}$



$f_0(500)$	π^0	$f_2(1270)$	
$f_0(980)$	η	$a_2(1320)$	
$a_0(980)$	$\eta'(958)$	$f_2'(1525)$	$f_4(2050)$
$f_0(1370)$	$\eta_c(1S)$	$f_2(1565)$	
$\chi_{c0}(1P)$	$\eta_c(2S)$	$a_2(1700)$	



s-channel diagrams (leading to peaks at $\sqrt{s} \cong m_M$)

t- and u-channels (leading to broad continua)

\Rightarrow P. Lebiedowicz, A. Szczurek,
The role of meson exchanges in light-by-light scattering,
Phys. Lett. **B772** (2017) 330

η & η' at UPC of AA...

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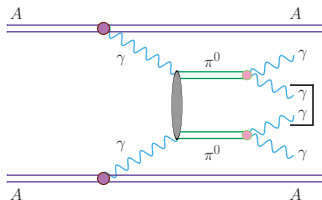
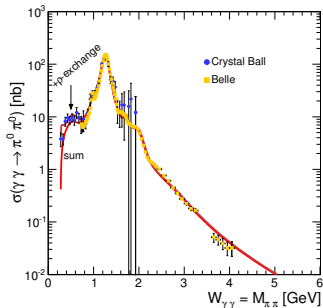
$M_{\gamma\gamma} < 5 \text{ GeV} \Rightarrow \pi^0\pi^0$ BACKGROUND

\Rightarrow M. K-G, A. Szczurek,
 $\pi^+\pi^-$ and $\pi^0\pi^0$ pair production in
 photon-photon and in ultraperipheral
 ultrarelativistic heavy ion collisions,
 Phys. Rev. **C87** (2013) 054908

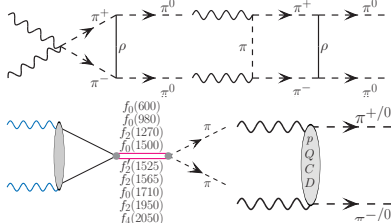
$\Rightarrow W_{\gamma\gamma} \in (2m_\pi - 6) \text{ GeV}$

\Rightarrow total cross section &
 angular distributions

\Rightarrow simultaneously for
 $\gamma\gamma \rightarrow \pi^+\pi^-$ & $\pi^0\pi^0$



$\gamma\gamma \rightarrow \pi^0\pi^0$



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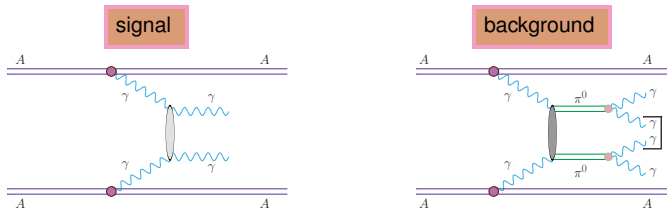
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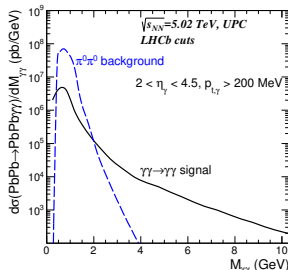
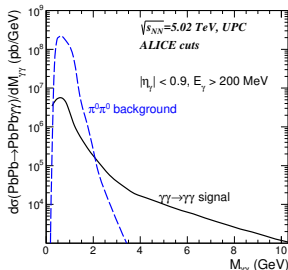
CONCLUSION

$AA \rightarrow AA \gamma\gamma$ FOR $M_{\gamma\gamma} < 5$ GeV ?

NEW



experiment	pseudorapidity range	other condition
ALICE	$-0.9 < \eta_\gamma < 0.9$	$E_\gamma > 200$ MeV
LHCb	$2.0 < \eta_\gamma < 4.5$	$p_{t,\gamma} > 200$ MeV

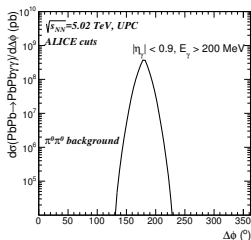
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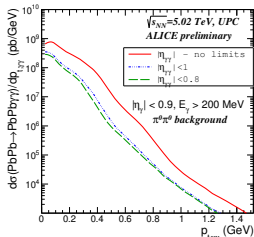
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CONCLUSION

$$\Delta\phi = \phi_{\gamma_1} - \phi_{\gamma_2}$$

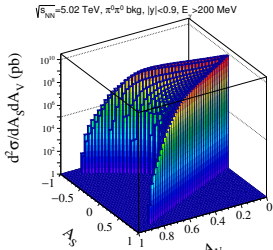


$$\vec{p}_{t,\gamma\gamma} = \vec{p}_{t,\gamma_1} + \vec{p}_{t,\gamma_2}$$

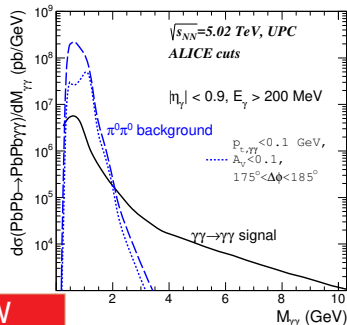


$$A_S = (|\vec{p}_{t1}| - |\vec{p}_{t2}|) / (|\vec{p}_{t1}| + |\vec{p}_{t2}|),$$

$$A_V = |\vec{p}_{t1} + \vec{p}_{t2}| / |\vec{p}_{t1} - \vec{p}_{t2}|$$



$$\Delta\phi \in (175 - 185)^\circ, |A_S/V| < 0.1, p_{t,\gamma\gamma} < 0.1 \text{ GeV}$$



NEW

CRACOVIAN
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EPA

$\gamma\gamma$ SCATTERING

FOUR-LEPTON
PRODUCTION

ELECTRONS
MUONS

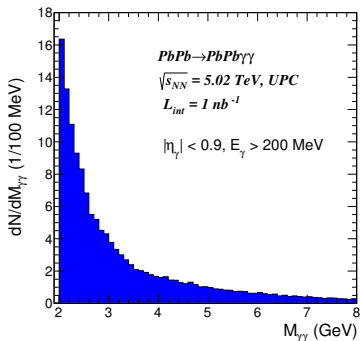
PRODUCTION

CONCLUSION

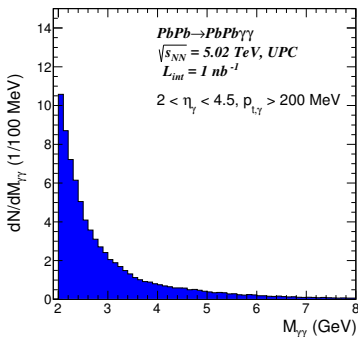
AA \rightarrow AA $\gamma\gamma$ FOR $M_{\gamma\gamma} > 2$ GeV ?

Our Predictions

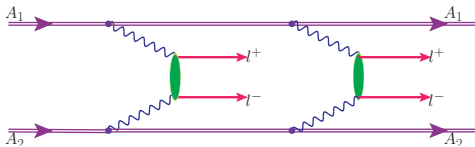
ALICE cuts



LHCb cuts



FOUR-LEPTON PRODUCTION



$$\begin{aligned}
 P_{AA \rightarrow AA l^+ l^-}^{\gamma\gamma}(b; y_{l^+}, y_{l^-}, p_{t,l}) &= \int N(\omega_1, \mathbf{b}_1) N(\omega_2, \mathbf{b}_2) S_{abs}^2(\mathbf{b}) \\
 &\times \frac{d\sigma_{\gamma\gamma \rightarrow l^+ l^-}(W_{\gamma\gamma})}{dz} d\bar{b}_x d\bar{b}_y \frac{W_{\gamma\gamma}}{2} dW_{\gamma\gamma} dY_{l_1 l_2} \\
 \frac{d\sigma_{A_1 A_2 \rightarrow A_1 A_2 l_1^+ l_2^- l_3^+ l_4^-}}{dy_{l^+} dy_{l^-} dp_{t,l} dy_{l^+} dy_{l^-} dp_{t,l}} &= \frac{1}{2} \int \frac{dP_{AA \rightarrow AA l^+ l^-}^I(b; y_{l^+}, y_{l^-}, p_{t,l})}{dy_{l^+} dy_{l^-} dp_{t,l}} \\
 &\times \frac{dP_{AA \rightarrow AA l^+ l^-}^{II}(b; y_{l^+}, y_{l^-}, p_{t,l})}{dy_{l^+} dy_{l^-} dp_{t,l}} d^2 b \\
 \sigma_{A_1 A_2 \rightarrow A_1 A_2 l^+ l^-} &= \int \frac{dP_{AA \rightarrow AA l^+ l^-}(b; y_{l^+}, y_{l^-}, p_{t,l})}{dy_{l^+} dy_{l^-} dp_{t,l}} d^2 b \\
 &\times dy_{l^+} dy_{l^-} dp_{t,l}
 \end{aligned}$$

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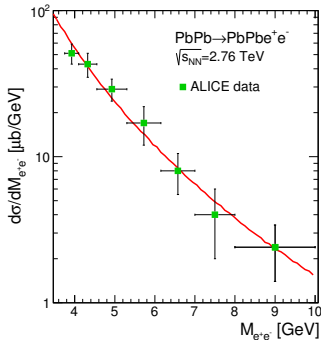
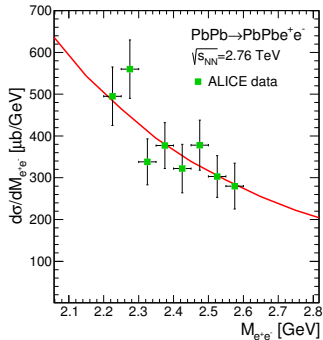
AA \rightarrow AAe⁺e⁻ - CALCULATIONS VS. DATA

- ALICE Collaboration (Abbas, E. et al.),
Charmonium and e⁺e⁻ pair photoproduction at mid-rapidity in ultra-peripheral Pb-Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV,
Eur. Phys. J. **C73** (2013) 2617

2.2 GeV < M_{ee} < 2.6 GeV

|y_e| < 0.9

3.7 GeV < M_{ee} < 10 GeV



Good description of single pair production \Rightarrow two e⁺e⁻ pair production

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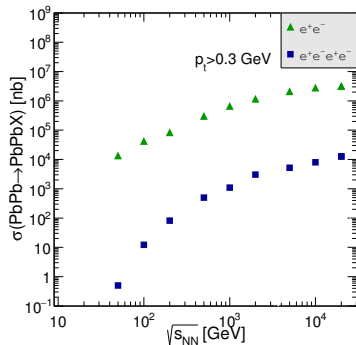
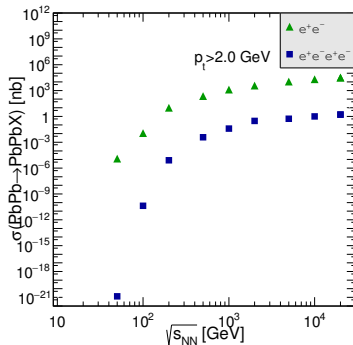
ELECTRONS

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CONCLUSION

$$AA \rightarrow AAe^+e^- \text{ \& \ } AA \rightarrow AAe^+e^-e^+e^-$$

 $p_t > 0.3 \text{ GeV}$

 $p_t > 2.0 \text{ GeV}$


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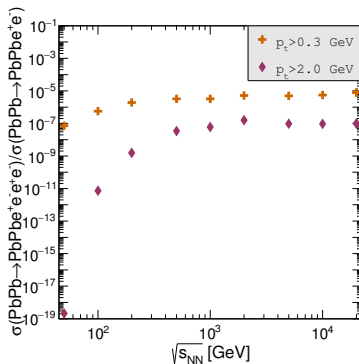
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$$AA \rightarrow AAe^+e^- \text{ \& \ } AA \rightarrow AAe^+e^-e^+e^-$$

$$\frac{\sigma_{AA \rightarrow AAe^+e^-e^+e^-}}{\sigma_{AA \rightarrow AAe^+e^-}}$$



Ratio depends on $\sqrt{s_{NN}}$ and $p_{t,min}$

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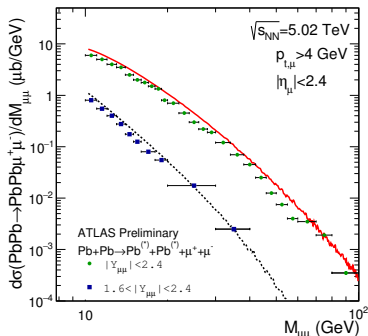
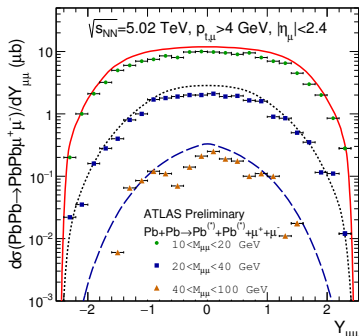
$AA \rightarrow AA\mu^+\mu^-$ - CALCULATIONS VS. DATA

- ATLAS Collaboration,
Measurement of high-mass dimuon pairs from ultraperipheral lead-lead collisions at $\sqrt{s_{NN}} = 5.02$ TeV with the ATLAS detector at the LHC, ATLAS-CONF-2016-025

$$\frac{d\sigma}{dY_{\mu^+\mu^-}}$$

$$p_{t,\mu} > 4 \text{ GeV}, |\eta_e| < 0.9$$

$$\frac{d\sigma}{dM_{\mu^+\mu^-}}$$



"Overwriting" of single $\mu^+\mu^-$ pair production

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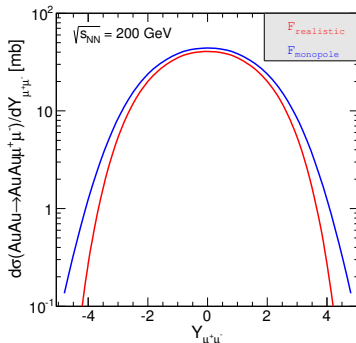
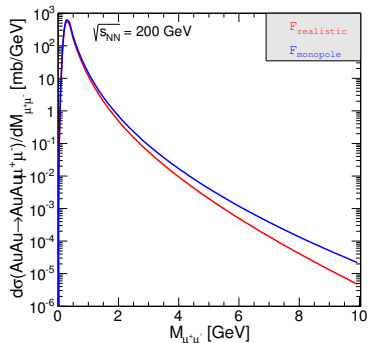
$AA \rightarrow AA \mu^+ \mu^-$ - FORM FACTOR

\Rightarrow realistic

\Rightarrow monopole

$M_{\mu^+ \mu^-}$

$Y_{\mu^+ \mu^-}$



RHIC energy

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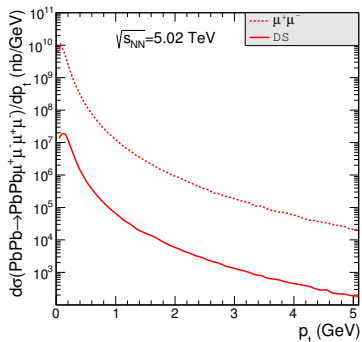
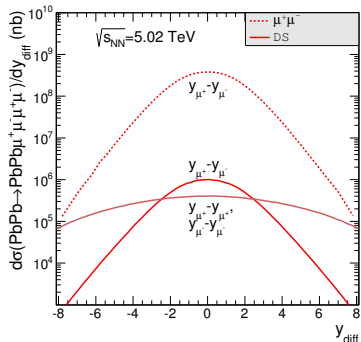
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$$AA \rightarrow AA\mu^+\mu^- \text{ \& \ } AA \rightarrow AA\mu^+\mu^-\mu^+\mu^-$$

 $p_{t,\mu}$

 y_{diff}


Similar like for electron-positron production: $\sigma_{\mu^+\mu^-} \simeq 1000 \times \sigma_{\mu^+\mu^-\mu^+\mu^-}$

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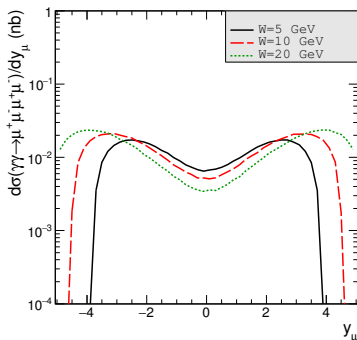
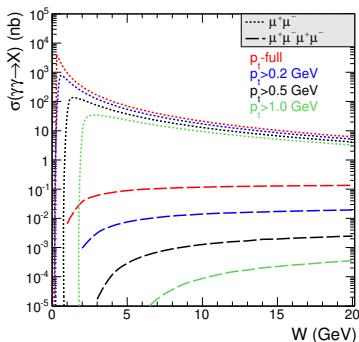
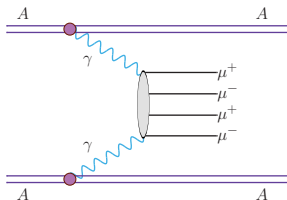
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$\gamma\gamma \rightarrow \mu^+\mu^-\mu^+\mu^-$ - SINGLE SCATTERING



KATIE - an event generator that is specially designed to deal with initial states that have an explicit transverse momentum dependence, but can also deal with on-shell initial states. KATIE is a parton-level generator for hadron scattering, but requires only a few adjustments to deal with photon scattering.



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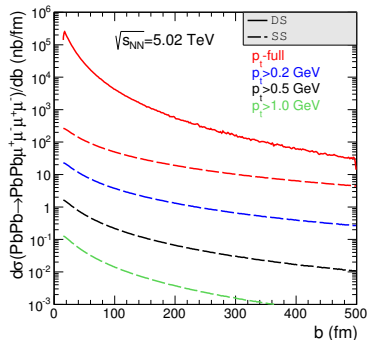
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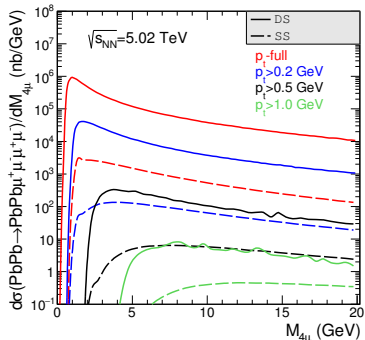
$$AA \rightarrow AA \mu^+ \mu^- \mu^+ \mu^-$$

impact parameter



↑ purely theoretical distribution

$W_{\gamma\gamma} = M_{4\mu}$



↑ DS dominates

It is difficult to isolate range of SS domination

- *DS - double-scattering mechanism
- *SS - a NEW single-scattering mechanism

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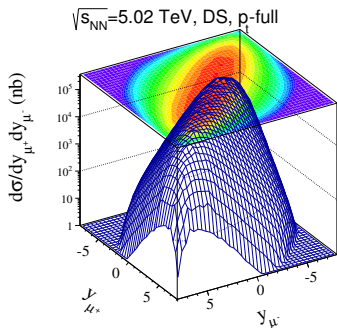
MUONS

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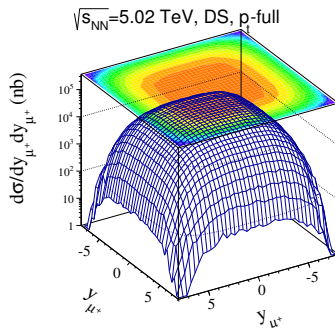
CONCLUSION

$$AA \rightarrow AA \mu^+ \mu^- \mu^+ \mu^-$$

$$y_{\mu^+}, y_{\mu^-}$$



$$y_{\mu^\pm}, y_{\mu^\pm}$$



$p_{t,\mu^+} \simeq p_{t,\mu^-} \Rightarrow$ construction of similar distributions by ALICE or CMS?

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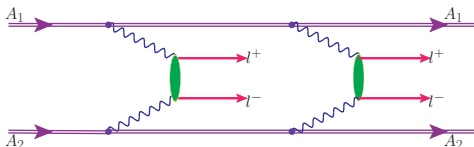
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The number of counts for $L_{int} = 1 \text{ nb}^{-1}$

$(4\mu), \sqrt{s_{NN}} = 5.02 \text{ TeV}$		$(4e), \sqrt{s_{NN}} = 5.5 \text{ TeV}$	
experimental cuts	N	experimental cuts	N
$ y_i < 2.5, p_t > 0.5 \text{ GeV}$	815	$ y_i < 2.5, p_t > 0.5 \text{ GeV}$	235
$ y_i < 2.5, p_t > 1.0 \text{ GeV}$	53	$ y_i < 2.5, p_t > 1.0 \text{ GeV}$	10
$ y_i < 0.9, p_t > 0.5 \text{ GeV}$	31	$ y_i < 1.0, p_t > 0.2 \text{ GeV}$	649
$ y_i < 0.9, p_t > 1.0 \text{ GeV}$	2	$ y_i < 1.0, p_t > 1.0 \text{ GeV}$	1
$ y_i < 2.4, p_t > 4.0 \text{ GeV}$	$\ll 1$		

CMS and ALICE $\Rightarrow p_{t,cut} = 1 \text{ GeV}$

ALICE $\Rightarrow p_{t,cut} = 0.2 \text{ GeV}$

ATLAS $\Rightarrow p_{t,cut} = 4 \text{ GeV}$ **Potential background**

$\downarrow \sqrt{s_{NN}} = 5.5 \text{ TeV}, |y| < 4.9$

Reaction	$p_{t,min} = 0.3 \text{ GeV}$	$p_{t,min} = 0.5 \text{ GeV}$
$PbPb \rightarrow PbPb\pi^+\pi^-\pi^+\pi^-$	2.954 mb	8.862 μb
$PbPb \rightarrow PbPbe^+e^-e^+e^-$	7.447 μb	0.704 μb

PROTON-ANTIPROTON PAIR PRODUCTION

$$\gamma(p_1, \lambda_1) + \gamma(p_2, \lambda_2) \rightarrow p(p_3, \lambda_3) + \bar{p}(p_4, \lambda_4)$$

$$\begin{aligned}
 \mathcal{M}_{\lambda_1 \lambda_2 \rightarrow \lambda_3 \lambda_4}^{p\text{-exchange}} &= (-i) \epsilon_{1\mu}(\lambda_1) \epsilon_{2\nu}(\lambda_2) \\
 &\times \bar{u}(p_3, \lambda_3) \left(i\Gamma^{(\gamma pp)}{}^\mu(p_3, p_t) \frac{i(\not{p}_t + m_p)}{t - m_p^2 + i\epsilon} i\Gamma^{(\gamma pp)}{}^\nu(p_t, -p_4) \right. \\
 &+ i\Gamma^{(\gamma pp)}{}^\nu(p_3, p_u) \frac{i(\not{p}_u + m_p)}{u - m_p^2 + i\epsilon} i\Gamma^{(\gamma pp)}{}^\mu(p_u, -p_4) \left. \right) v(p_4, \lambda_4)
 \end{aligned}$$

$$\begin{aligned}
 \mathcal{M}_{\lambda_1 \lambda_2 \rightarrow \lambda_3 \lambda_4}^{f_2(1270), f_2(1950)} &= (-i) \epsilon_{1\mu}(\lambda_1) \epsilon_{2\nu}(\lambda_2) i\Gamma^{(f_2 \gamma \gamma)}{}^{\mu\nu\kappa\lambda}(p_1, p_2) i\Delta_{\kappa\lambda, \alpha\beta}^{(f_2)}(p_s) \\
 &\times \bar{u}(p_3, \lambda_3) i\Gamma^{(f_2 p \bar{p})}{}^{\alpha\beta}(p_3, p_4) v(p_4, \lambda_4)
 \end{aligned}$$

> M. Diehl, P. Kroll, and C. Vogt,
Two-photon annihilation into baryon anti-baryon pairs,
 Eur. Phys. J. **C26** (2003) 567

Free parameters: off-shell form factors, the coupling constants.

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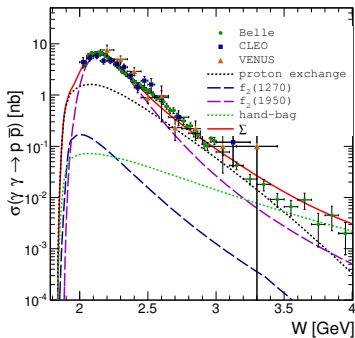
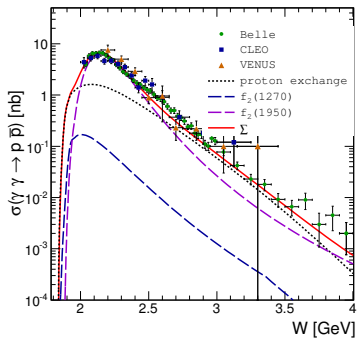
MUONS

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$\gamma\gamma \rightarrow p\bar{p}$ - RESULTS VS. DATA

$$|\cos\theta| < 0.6$$

 \dagger hand-bag model


Good description of $\sigma(W)$ data $\Rightarrow \frac{d\sigma}{dz}$?

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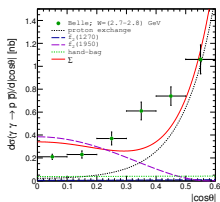
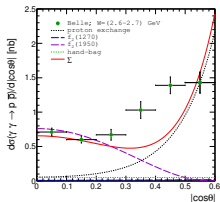
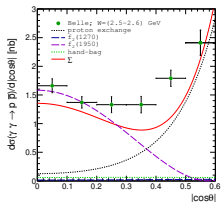
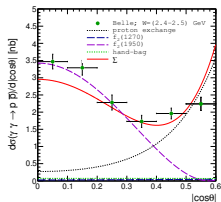
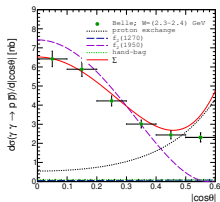
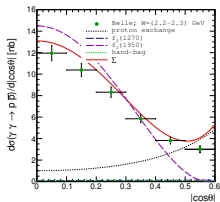
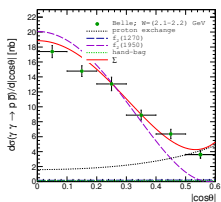
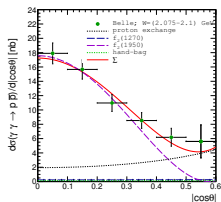
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ANGULAR DISTRIBUTIONS

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without hand-bag

with hand-bag model

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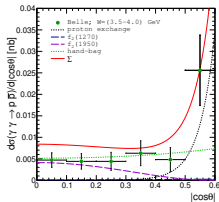
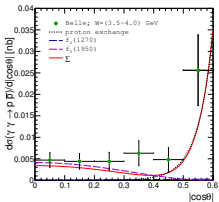
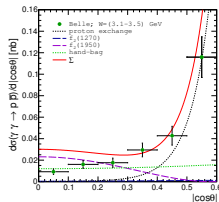
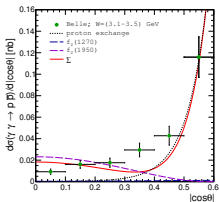
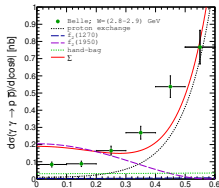
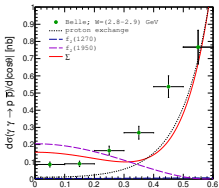
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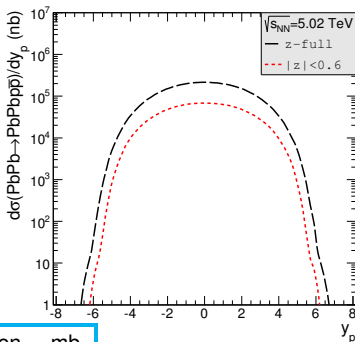
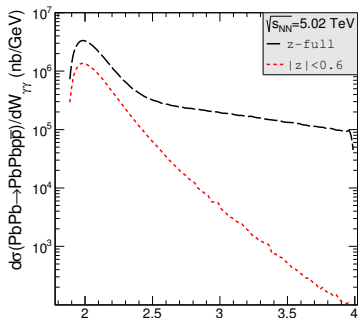
CONCLUSION



AA \rightarrow AAp \bar{p} RESULTS

$$W_{\gamma\gamma} = M_{p\bar{p}}$$

$$y_p$$



Cross section \sim mb

Can be studied by ALICE, ATLAS, CMS group?

Experiment	Cuts	σ [μ b]
ALICE	$p_{t,p} > 0.2$ GeV, $ y_p < 0.9$	100
ATLAS	$p_{t,p} > 0.5$ GeV, $ y_p < 2.5$	160
CMS	$p_{t,p} > 0.2$ GeV, $ y_p < 2.5$	500
LHCb	$p_{t,p} > 0.2$ GeV, $2 < y_p < 4.5$	104

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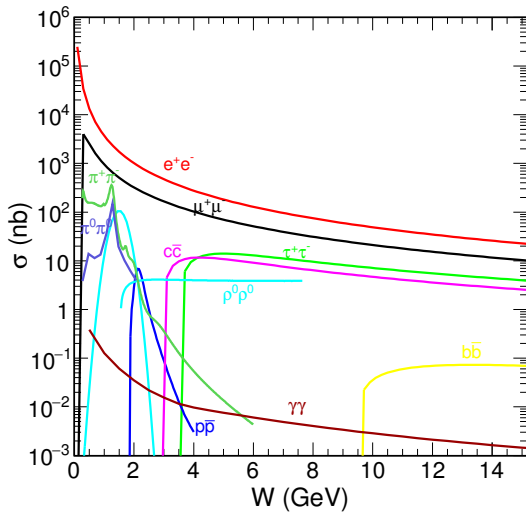
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CONCLUSION

- EPA in **the impact parameter space**
- $\gamma\gamma \rightarrow X_1 X_2 (X_3 X_4)$
- **Realistic charge distribution**
- Description of the ATLAS data for $Pb Pb \rightarrow Pb Pb \gamma\gamma$ & for ALICE and ATLAS data for $Pb Pb \rightarrow Pb Pb l^+ l^-$
- $Pb Pb \rightarrow Pb Pb \mu^+ \mu^- \mu^+ \mu^- \Rightarrow \sigma_{SS}^{NEW} < \sigma_{DS}$
- Difficult to isolate a region **where SS dominates**
- $\sigma_{AA \rightarrow AA l^+ l^-} \cong 1000 \times \sigma_{AA \rightarrow AA l^+ l^- l^+ l^-}$
- The cross sections for four-lepton production strongly **depend on the $p_{t,min}$ and y_l**
- Light-by-light scattering in UPC for $M_{\gamma\gamma} < 5 \text{ GeV}$ - **new project**

$\gamma\gamma \rightarrow X_1 X_2$ - REVIEW

Thank you

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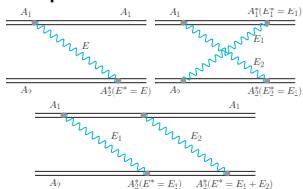
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BACKUP SLIDES

Multiple Coulomb excitations

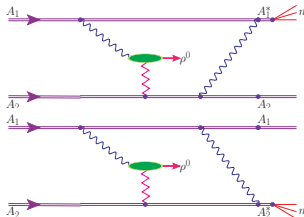
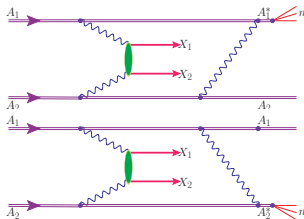
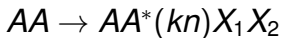
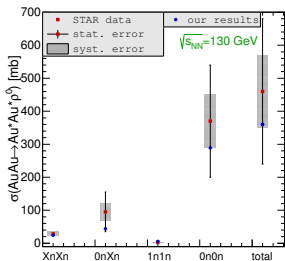


Ref.

M. Kłusek-Gawenda, M. Ciemala, W. Schäfer and A. Szczurek,
Phys. Rev. **C89** (2014) 054907,

"Electromagnetic excitation of nuclei and neutron evaporation
in ultrarelativistic ultraperipheral heavy ion collisions"

ρ^0 production in heavy ion UPC with nuclear excitation



CRACOVIAN
THEORETICAL
RESULTS FOR UPC

EPA

$\gamma\gamma$ SCATTERING

FOUR-LEPTON
PRODUCTION

ELECTRONS

MUONS

PROTON-
ANTIPROTON
PRODUCTION

CONCLUSION

$$A(m) = \mathcal{A}_{\text{BW}} \frac{\sqrt{m m_{\rho^0} \Gamma_{\rho^0}(m)}}{m^2 - m_{\rho^0}^2 + i m_{\rho^0} \Gamma_{\rho^0}(m)} + \mathcal{B}_{\pi\pi}$$

$$\text{running width: } \Gamma_{\rho^0}(m) = \Gamma_{\rho^0} \frac{m_{\rho^0}}{m} \left(\frac{m^2 - 4m_{\pi}^2}{m_{\rho^0}^2 - 4m_{\pi}^2} \right)^{3/2}$$

Drell-Söding + $f_2(1270)$

colored solid lines -

$$\Gamma_{\rho^0} = 150.2 \text{ MeV}$$

colored dashed lines -

$$\Gamma_{\rho^0} = 140 \text{ MeV}$$

- ALICE Collaboration,
Coherent ρ^0 photoproduction in ultra-peripheral Pb-Pb collisions at $\sqrt{s_{\text{NN}}} = 2.76 \text{ TeV}$, JHEP 1509 (2015) 095

